

# Algebra I Vocabulary Cards

## Table of Contents

### **Expressions and Operations**

Natural Numbers  
Whole Numbers  
Integers  
Rational Numbers  
Irrational Numbers  
Real Numbers  
Absolute Value  
Order of Operations  
Expression  
Variable  
Coefficient  
Term  
Scientific Notation  
Exponential Form  
Negative Exponent  
Zero Exponent  
Product of Powers Property  
Power of a Power Property  
Power of a Product Property  
Quotient of Powers Property  
Power of a Quotient Property  
Polynomial  
Degree of Polynomial  
Leading Coefficient  
Add Polynomials (group like terms)  
Add Polynomials (align like terms)  
Subtract Polynomials (group like terms)  
Subtract Polynomials (align like terms)  
Multiply Polynomials  
Multiply Binomials  
Multiply Binomials (model)  
Multiply Binomials (graphic organizer)  
Multiply Binomials (squaring a binomial)  
Multiply Binomials (sum and difference)  
Factors of a Monomial  
Factoring (greatest common factor)  
Factoring (perfect square trinomials)  
Factoring (difference of squares)  
Difference of Squares (model)  
Divide Polynomials (monomial divisor)  
Divide Polynomials (binomial divisor)  
Prime Polynomial

Square Root  
Cube Root  
Product Property of Radicals  
Quotient Property of Radicals  
Zero Product Property  
Solutions or Roots  
Zeros  
x-Intercepts

### **Equations and Inequalities**

Coordinate Plane  
Linear Equation  
Linear Equation (standard form)  
Literal Equation  
Vertical Line  
Horizontal Line  
Quadratic Equation  
Quadratic Equation (solve by factoring)  
Quadratic Equation (solve by graphing)  
Quadratic Equation (number of solutions)  
Identity Property of Addition  
Inverse Property of Addition  
Commutative Property of Addition  
Associative Property of Addition  
Identity Property of Multiplication  
Inverse Property of Multiplication  
Commutative Property of Multiplication  
Associative Property of Multiplication  
Distributive Property  
Distributive Property (model)  
Multiplicative Property of Zero  
Substitution Property  
Reflexive Property of Equality  
Symmetric Property of Equality  
Transitive Property of Equality  
Inequality  
Graph of an Inequality  
Transitive Property for Inequality  
Addition/Subtraction Property of Inequality  
Multiplication Property of Inequality  
Division Property of Inequality  
Linear Equation (slope intercept form)  
Linear Equation (point-slope form)

Slope  
Slope Formula  
Slopes of Lines  
Perpendicular Lines  
Parallel Lines  
Mathematical Notation  
System of Linear Equations (graphing)  
System of Linear Equations (substitution)  
System of Linear Equations (elimination)  
System of Linear Equations (number of solutions)  
Graphing Linear Inequalities  
System of Linear Inequalities  
Dependent and Independent Variable  
Dependent and Independent Variable (application)  
Graph of a Quadratic Equation  
Quadratic Formula

## **Relations and Functions**

Relations (examples)  
Functions (examples)  
Function (definition)  
Domain  
Range  
Function Notation  
Parent Functions

- Linear, Quadratic

Transformations of Parent Functions

- Translation
- Reflection
- Dilation

Linear Function (transformational graphing)

- Translation
- Dilation ( $m > 0$ )
- Dilation/reflection ( $m < 0$ )

Quadratic Function (transformational graphing)

- Vertical translation
- Dilation ( $a > 0$ )
- Dilation/reflection ( $a < 0$ )
- Horizontal translation

Direct Variation  
Inverse Variation

## **Statistics**

Statistics Notation  
Mean  
Median  
Mode  
Box-and-Whisker Plot  
Summation

Mean Absolute Deviation  
Variance  
Standard Deviation (definition)  
z-Score (definition)  
z-Score (graphic)  
Elements within One Standard Deviation of the Mean (graphic)  
Scatterplot  
Positive Correlation  
Negative Correlation  
No Correlation  
Curve of Best Fit (linear/quadratic)  
Outlier Data (graphic)

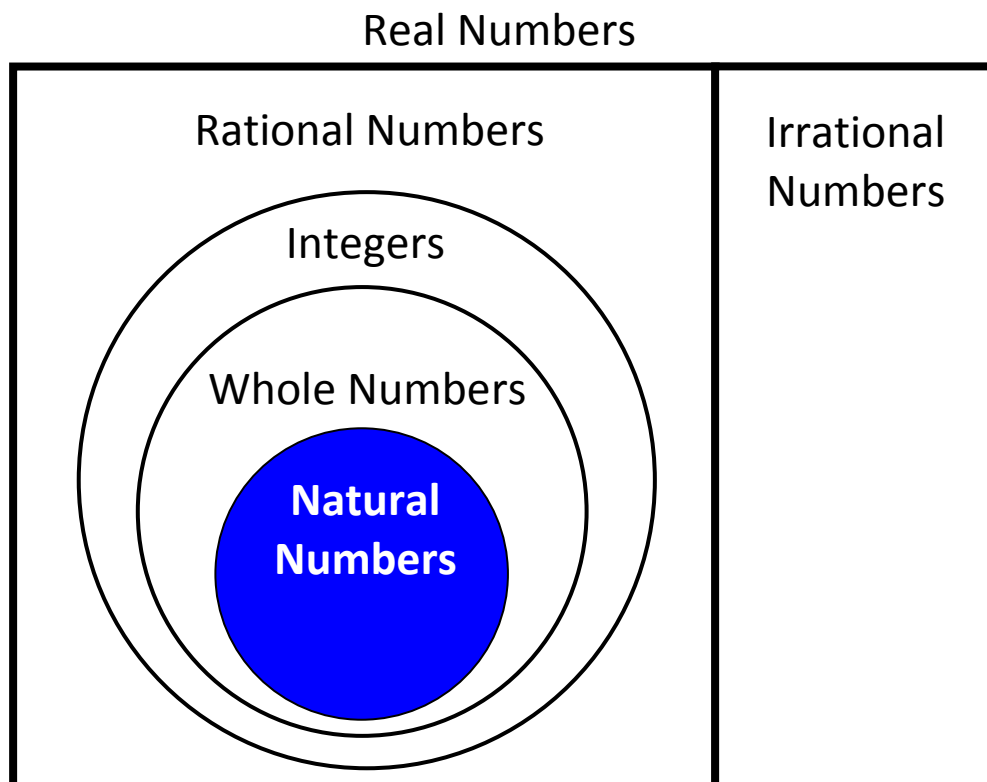
### Revisions:

October 2014 – removed Constant Correlation;  
removed negative sign on Linear Equation  
(slope intercept form)

July 2015 – Add Polynomials (removed  
exponent); Subtract Polynomials (added  
negative sign); Multiply Polynomials (graphic  
organizer)( $16x$  and  $13x$ ); Z-Score (added  $z = 0$ )

# Natural Numbers

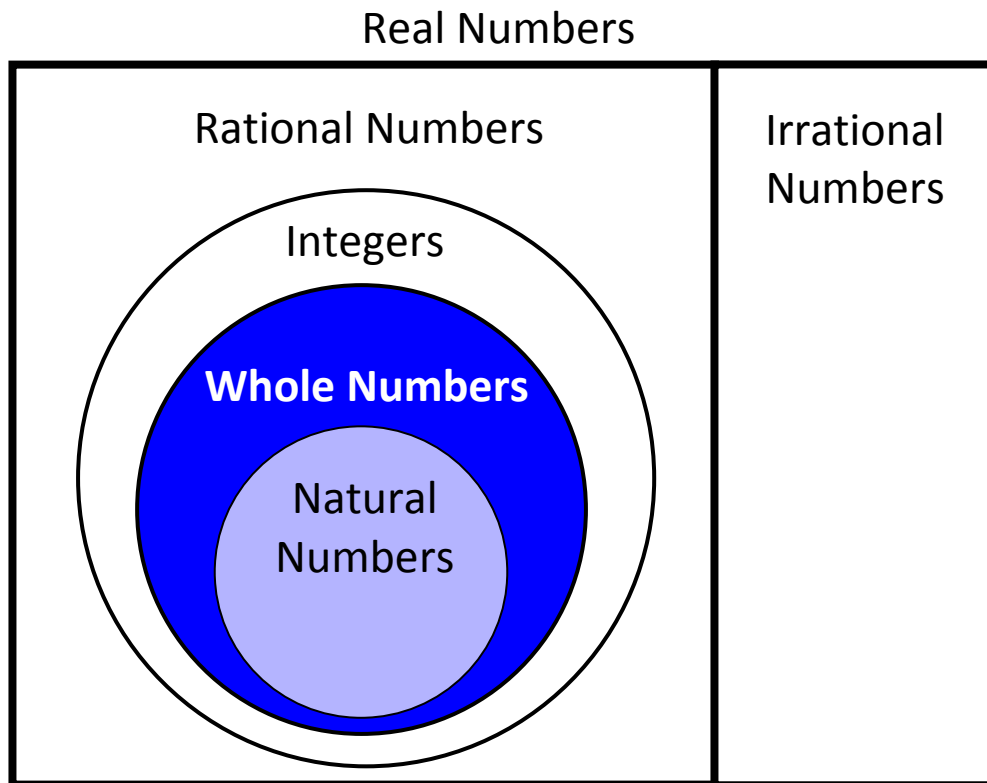
The set of numbers  
1, 2, 3, 4...



# Whole Numbers

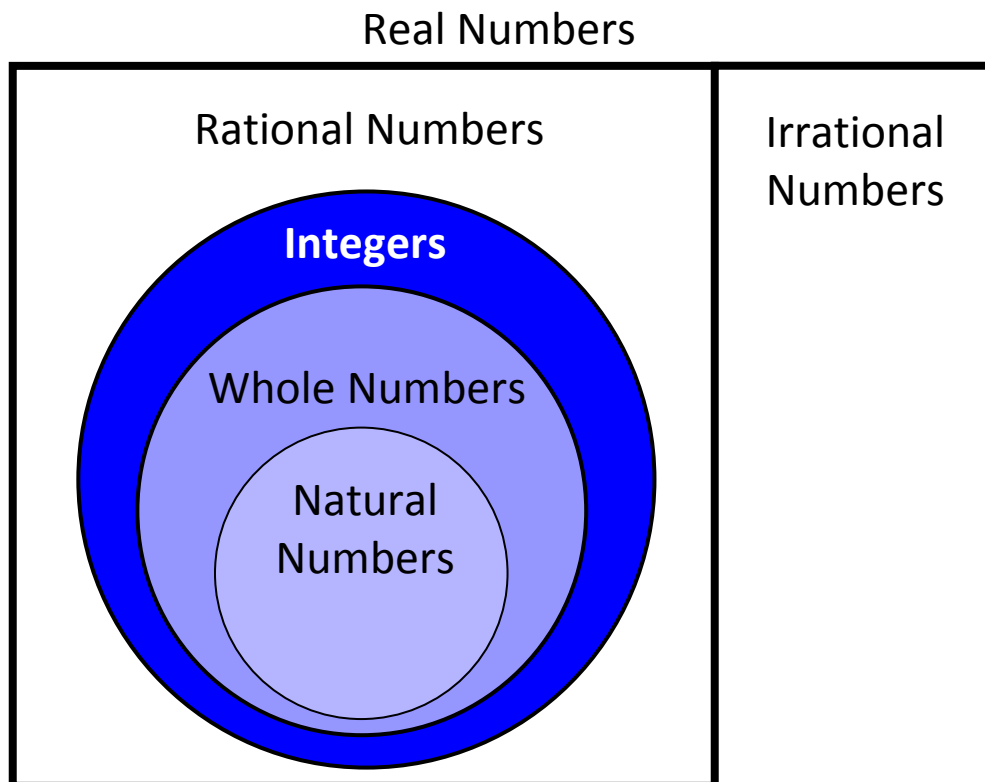
The set of numbers

0, 1, 2, 3, 4...

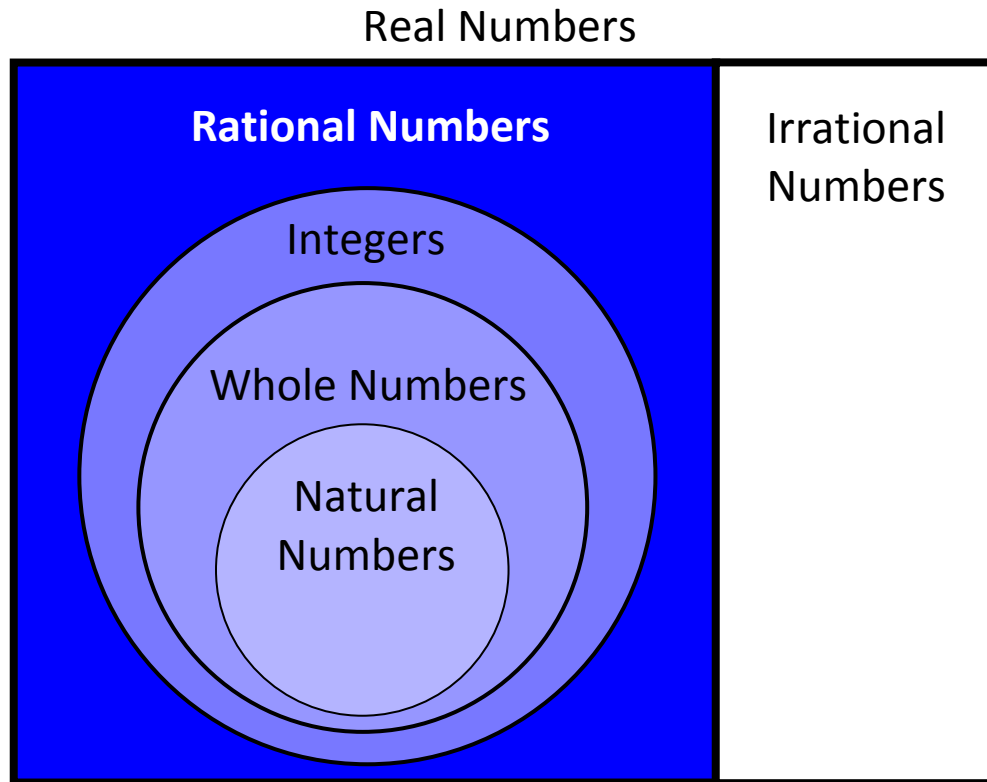


# Integers

The set of numbers  
...-3, -2, -1, 0, 1, 2, 3...



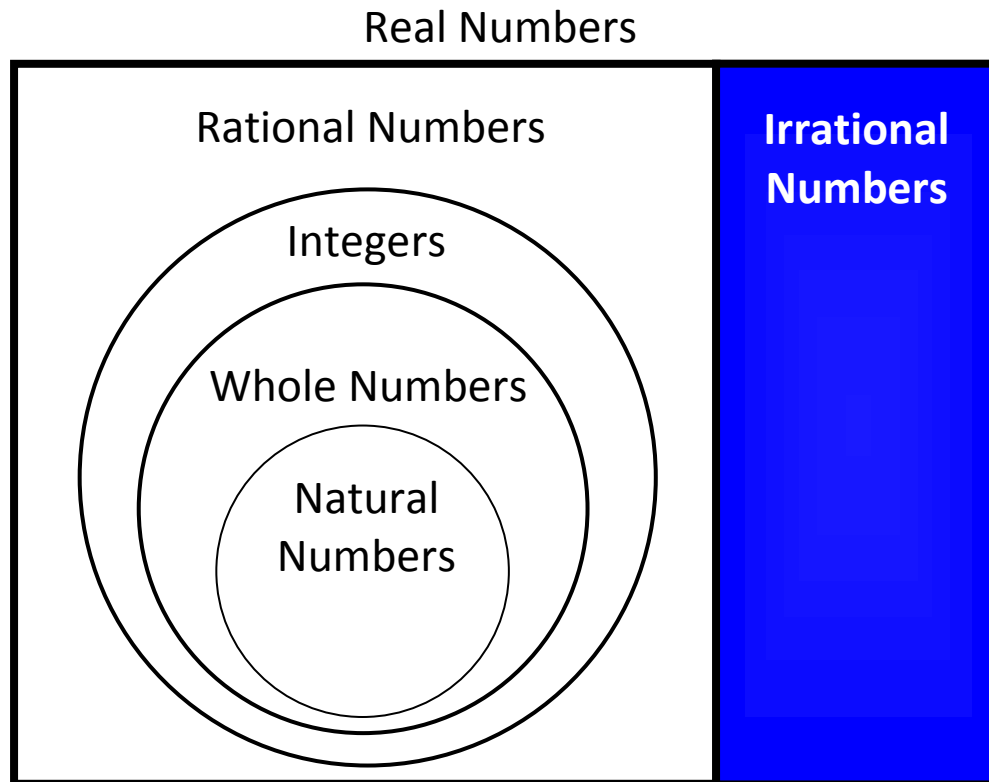
# Rational Numbers



The set of all numbers that can be written as the ratio of two integers with a non-zero denominator

$$2\frac{3}{5}, -5, 0.3, \sqrt{16}, \frac{13}{7}$$

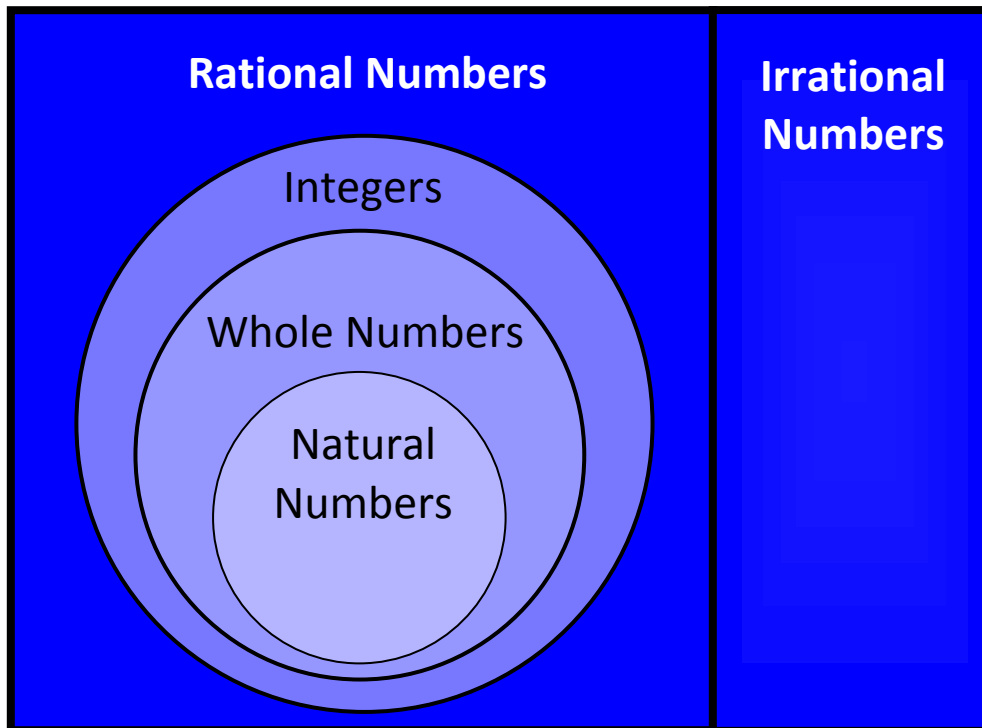
# Irrational Numbers



The set of all numbers that cannot be expressed as the ratio of integers

$$\sqrt{7}, \pi, -0.23223222322223...$$

# Real Numbers



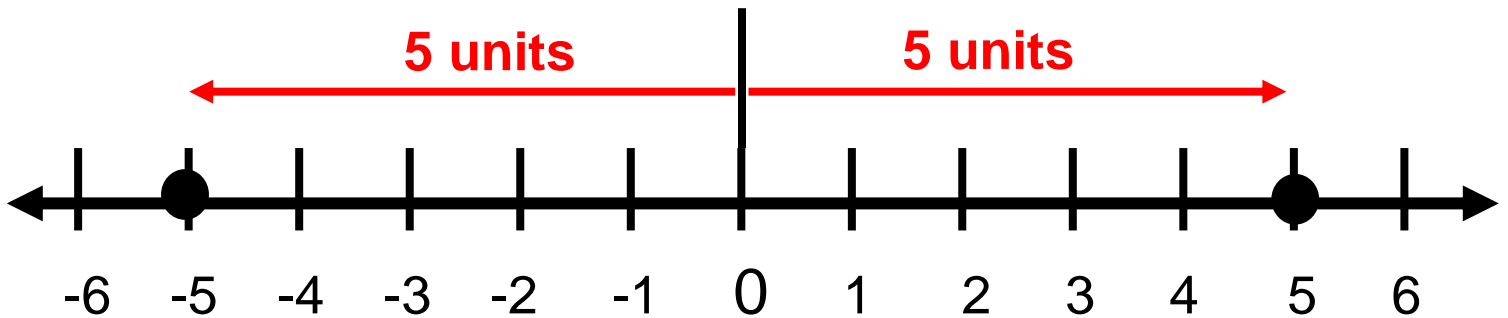
The set of all rational and irrational numbers



# Absolute Value

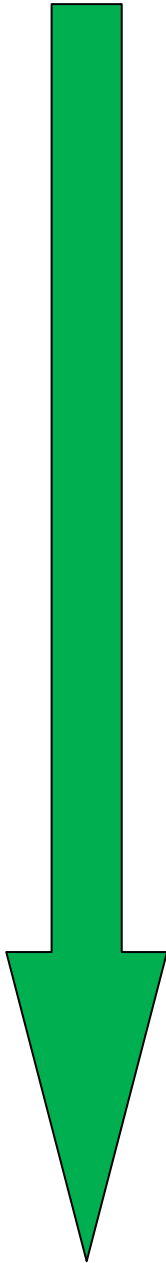
$$|5| = 5$$

$$|-5| = 5$$



The distance between a number  
and zero

# Order of Operations



<b>G</b> rouping Symbols	$()$ $\{\}$ $[\ ]$  absolute value  fraction bar
<b>E</b> xponents	$a^n$
<b>M</b> ultiplication <b>D</b> ivision	$\longrightarrow$ Left to Right
<b>A</b> ddition <b>S</b> ubtraction	$\longrightarrow$ Left to Right

# Expression

$x$

$-\sqrt{26}$

$3^4 + 2m$

$3(y + 3.9)^2 - \frac{8}{9}$

# Variable

$$2(y + \sqrt{3})$$

$$9 + x = 2.08$$

$$d = 7c - 5$$

$$A = \pi r^2$$

# Coefficient

$$(-4) + 2x$$

$$-7y^2$$

$$\frac{2}{3}ab - \frac{1}{2}$$

$$\pi r^2$$

# Term

$$\underbrace{3x} + \underbrace{2y} - \underbrace{8}$$

3 terms

$$\underbrace{-5x^2} - \underbrace{x}$$

2 terms

$$\underbrace{\frac{2}{3}ab}$$

1 term

# Scientific Notation

$$a \times 10^n$$

$1 \leq |a| < 10$  and  $n$  is an integer

Examples:

Standard Notation	Scientific Notation
17,500,000	$1.75 \times 10^7$
-84,623	$-8.4623 \times 10^4$
0.0000026	$2.6 \times 10^{-6}$
-0.080029	$-8.0029 \times 10^{-2}$

# Exponential Form

$$a^n = \underbrace{a \cdot a \cdot a \cdot a \dots}_{\text{factors}}, a \neq 0$$

Diagram illustrating the exponential form  $a^n$ . The base  $a$  is labeled "base" and the exponent  $n$  is labeled "exponent". The expression is shown as a product of  $n$  factors of  $a$ , with a bracket under the first four  $a$ 's labeled "factors".

Examples:

$$2 \cdot 2 \cdot 2 = 2^3 = 8$$

$$n \cdot n \cdot n \cdot n = n^4$$

$$3 \cdot 3 \cdot 3 \cdot x \cdot x = 3^3 x^2 = 27x^2$$



# Negative Exponent

$$a^{-n} = \frac{1}{a^n}, a \neq 0$$

Examples:

$$4^{-2} = \frac{1}{4^2} = \frac{1}{16}$$

$$\frac{x^4}{y^{-2}} = \frac{x^4}{\frac{1}{y^2}} = \frac{x^4}{1} \cdot \frac{y^2}{y^2} = x^4 y^2$$

$$(2 - a)^{-2} = \frac{1}{(2 - a)^2}, a \neq 2$$

# Zero Exponent

$$a^0 = 1, a \neq 0$$

Examples:

$$(-5)^0 = 1$$

$$(3x + 2)^0 = 1$$

$$(x^2 y^{-5} z^8)^0 = 1$$

$$4m^0 = 4 \cdot 1 = 4$$

# Product of Powers Property

$$a^m \cdot a^n = a^{m+n}$$

Examples:

$$x^4 \cdot x^2 = x^{4+2} = x^6$$

$$a^3 \cdot a = a^{3+1} = a^4$$

$$w^7 \cdot w^{-4} = w^{7+(-4)} = w^3$$

# Power of a Power Property

$$(a^m)^n = a^{m \cdot n}$$

Examples:

$$(y^4)^2 = y^{4 \cdot 2} = y^8$$

$$(g^2)^{-3} = g^{2 \cdot (-3)} = g^{-6} = \frac{1}{g^6}$$

# Power of a Product Property

$$(ab)^m = a^m \cdot b^m$$

Examples:

$$(-3ab)^2 = (-3)^2 \cdot a^2 \cdot b^2 = 9a^2b^2$$

$$\frac{-1}{(2x)^3} = \frac{-1}{2^3 \cdot x^3} = \frac{-1}{8x^3}$$

# Quotient of Powers Property

$$\frac{a^m}{a^n} = a^{m-n}, \quad a \neq 0$$

Examples:

$$\frac{x^6}{x^5} = x^{6-5} = x^1 = x$$

$$\frac{y^{-3}}{y^{-5}} = y^{-3-(-5)} = y^2$$

$$\frac{a^4}{a^4} = a^{4-4} = a^0 = 1$$

# Power of Quotient Property

$$\left(\frac{a}{b}\right)^m = \frac{a^m}{b^m}, \quad b \neq 0$$

Examples:

$$\left(\frac{y}{3}\right)^4 = \frac{y^4}{3^4}$$

$$\left(\frac{5}{t}\right)^{-3} = \frac{5^{-3}}{t^{-3}} = \frac{\frac{1}{5^3}}{\frac{1}{t^3}} = \frac{t^3}{5^3} = \frac{t^3}{125}$$

# Polynomial

Example	Name	Terms
$7$ $6x$	monomial	1 term
$3t - 1$ $12xy^3 + 5x^4y$	binomial	2 terms
$2x^2 + 3x - 7$	trinomial	3 terms

Nonexample	Reason
$5m^n - 8$	variable exponent
$n^{-3} + 9$	negative exponent



# Degree of a Polynomial

The largest exponent or the largest sum of exponents of a term within a polynomial

Example:

$$6a^3 + 3a^2b^3 - 21$$

Term	Degree
$6a^3$	3
$3a^2b^3$	5
-21	0

**Degree of polynomial:**

**5**

# Leading Coefficient

The coefficient of the first term of a polynomial written in descending order of exponents

Examples:

$$7a^3 - 2a^2 + 8a - 1$$

$$-3n^3 + 7n^2 - 4n + 10$$

$$16t - 1$$

# Add Polynomials

Combine like terms.

Example:

$$(2g^2 + 6g - 4) + (g^2 - g)$$
$$= 2g^2 + 6g - 4 + g^2 - g$$

(Group like terms and add.)

$$= (2g^2 + g^2) + (6g - g) - 4$$
$$= 3g^2 + 5g - 4$$

# Add Polynomials

Combine like terms.

Example:

$$(2g^3 + 6g^2 - 4) + (g^3 - g - 3)$$

(Align like terms and add.)

$$\begin{array}{r} 2g^3 + 6g^2 \quad - 4 \\ + \quad g^3 \quad - g - 3 \\ \hline 3g^3 + 6g^2 - g - 7 \end{array}$$

# Subtract Polynomials

Add the inverse.

Example:

$$(4x^2 + 5) - (-2x^2 + 4x - 7)$$

(Add the inverse.)

$$= (4x^2 + 5) + (2x^2 - 4x + 7)$$

$$= 4x^2 + 5 + 2x^2 - 4x + 7$$

(Group like terms and add.)

$$= (4x^2 + 2x^2) - 4x + (5 + 7)$$

$$= 6x^2 - 4x + 12$$



# Multiply Polynomials

Apply the distributive property.

$$(a + b)(d + e + f)$$

$$(a + b)(d + e + f)$$

$$= a(d + e + f) + b(d + e + f)$$

$$= ad + ae + af + bd + be + bf$$

# Multiply Binomials

Apply the distributive property.

$$\begin{aligned}(a + b)(c + d) &= \\ a(c + d) + b(c + d) &= \\ ac + ad + bc + bd &\end{aligned}$$

Example:  $(x + 3)(x + 2)$

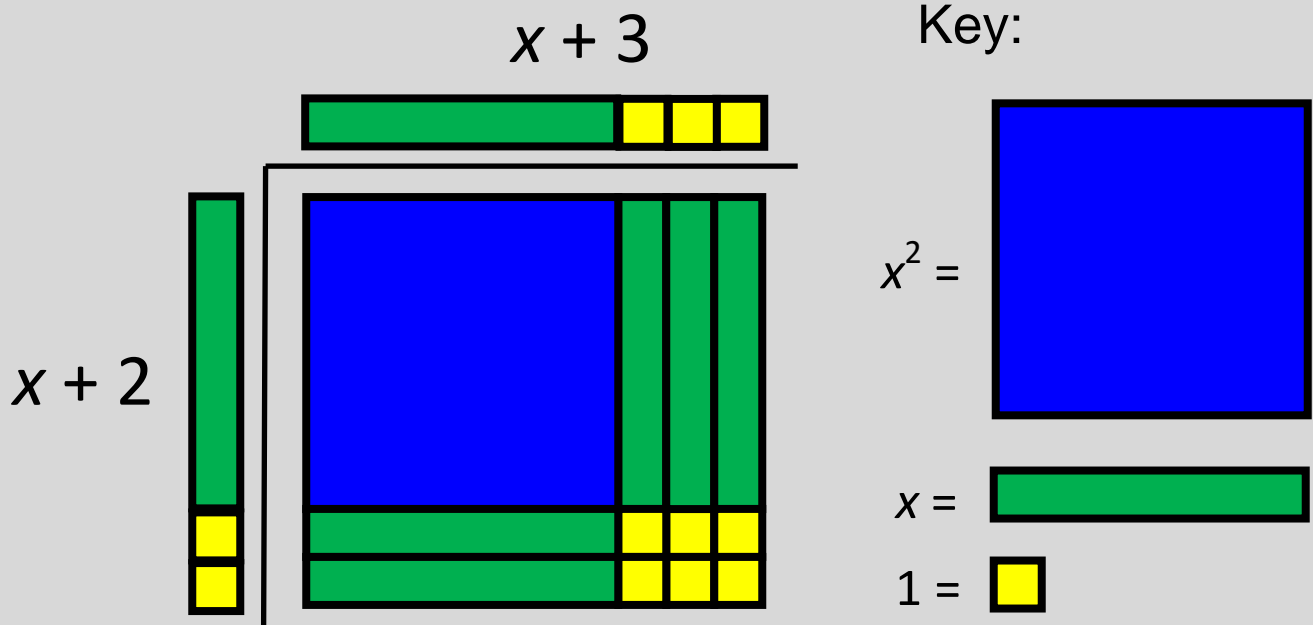
$$\begin{aligned}&= x(x + 2) + 3(x + 2) \\ &= x^2 + 2x + 3x + 6 \\ &= x^2 + 5x + 6\end{aligned}$$



# Multiply Binomials

Apply the distributive property.

Example:  $(x + 3)(x + 2)$



$$x^2 + 2x + 3x + 6 = x^2 + 5x + 6$$

# Multiply Binomials

Apply the distributive property.

$$\begin{aligned}\text{Example: } & (x + 8)(2x - 3) \\ & = (x + 8)(2x + -3)\end{aligned}$$

	$2x$	$+$	$-3$
$x$	$2x^2$		$-3x$
$+$			
$8$	$16x$		$-24$

$$2x^2 + 16x + -3x + -24 = 2x^2 + 13x - 24$$

# Multiply Binomials: Squaring a Binomial

$$(a + b)^2 = a^2 + 2ab + b^2$$

$$(a - b)^2 = a^2 - 2ab + b^2$$

Examples:

$$\begin{aligned}(3m + n)^2 &= 9m^2 + 2(3m)(n) + n^2 \\ &= 9m^2 + 6mn + n^2\end{aligned}$$

$$\begin{aligned}(y - 5)^2 &= y^2 - 2(5)(y) + 25 \\ &= y^2 - 10y + 25\end{aligned}$$

# Multiply Binomials: Sum and Difference

$$(a + b)(a - b) = a^2 - b^2$$

Examples:

$$(2b + 5)(2b - 5) = 4b^2 - 25$$

$$\begin{aligned}(7 - w)(7 + w) &= 49 + 7w - 7w - w^2 \\ &= 49 - w^2\end{aligned}$$

# Factors of a Monomial

The number(s) and/or variable(s) that are multiplied together to form a monomial

Examples:	Factors	Expanded Form
$5b^2$	$5 \cdot b^2$	$5 \cdot b \cdot b$
$6x^2y$	$6 \cdot x^2 \cdot y$	$2 \cdot 3 \cdot x \cdot x \cdot y$
$\frac{-5p^2q^3}{2}$	$\frac{-5}{2} \cdot p^2 \cdot q^3$	$\frac{1}{2} \cdot (-5) \cdot p \cdot p \cdot q \cdot q \cdot q$

# Factoring: Greatest Common Factor

Find the greatest common factor (GCF) of all terms of the polynomial and then apply the distributive property.

Example:  $20a^4 + 8a$

$$\textcircled{2} \cdot \textcircled{2} \cdot 5 \cdot \textcircled{a} \cdot a \cdot a \cdot a + \textcircled{2} \cdot \textcircled{2} \cdot 2 \cdot \textcircled{a}$$

common factors

$$\text{GCF} = \overbrace{2 \cdot 2 \cdot a} = 4a$$

$$20a^4 + 8a = 4a(5a^3 + 2)$$

# Factoring: Perfect Square Trinomials

$$a^2 + 2ab + b^2 = (a + b)^2$$

$$a^2 - 2ab + b^2 = (a - b)^2$$

Examples:

$$\begin{aligned}x^2 + 6x + 9 &= x^2 + 2 \cdot 3 \cdot x + 3^2 \\ &= (x + 3)^2\end{aligned}$$

$$\begin{aligned}4x^2 - 20x + 25 &= (2x)^2 - 2 \cdot 2x \cdot 5 + 5^2 \\ &= (2x - 5)^2\end{aligned}$$

# Factoring: Difference of Two Squares

$$a^2 - b^2 = (a + b)(a - b)$$

Examples:

$$x^2 - 49 = x^2 - 7^2 = (x + 7)(x - 7)$$

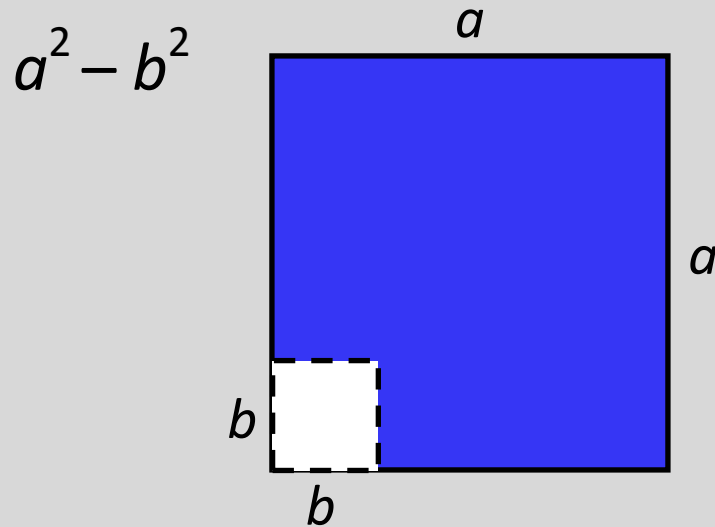
$$4 - n^2 = 2^2 - n^2 = (2 - n)(2 + n)$$

$$\begin{aligned} 9x^2 - 25y^2 &= (3x)^2 - (5y)^2 \\ &= (3x + 5y)(3x - 5y) \end{aligned}$$

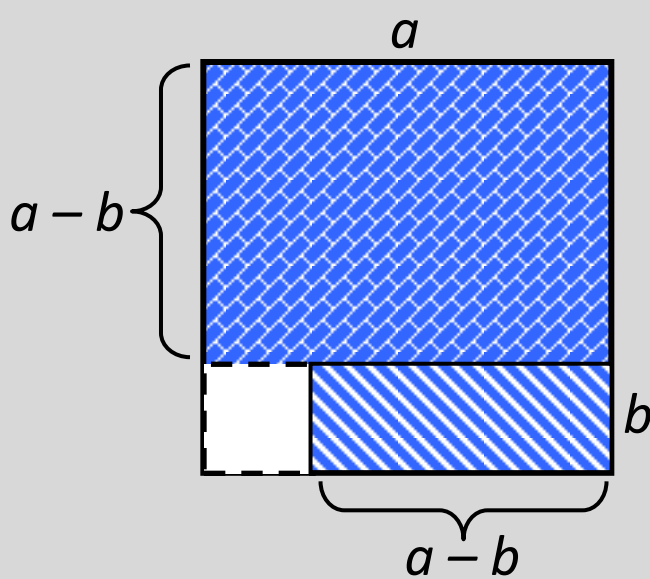


# Difference of Squares

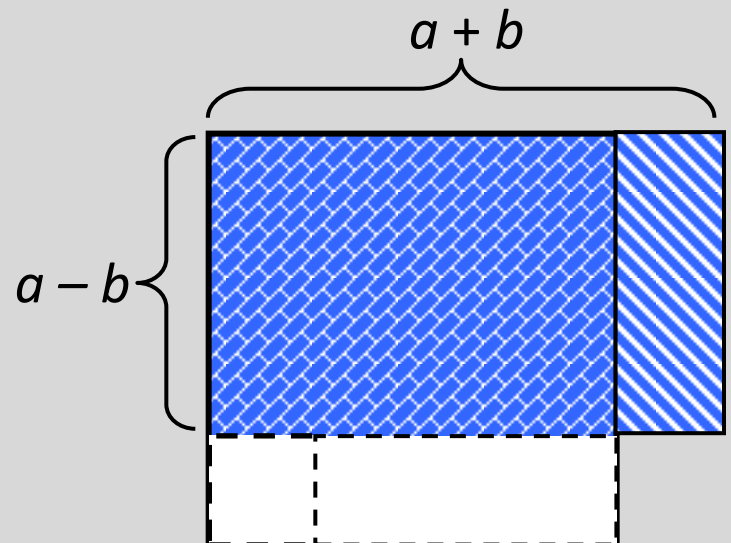
$$a^2 - b^2 = (a + b)(a - b)$$



$$a(a - b) + b(a - b)$$



$$(a + b)(a - b)$$



# Divide Polynomials

Divide each term of the dividend  
by the monomial divisor

Example:

$$(12x^3 - 36x^2 + 16x) \div 4x$$

$$= \frac{12x^3 - 36x^2 + 16x}{4x}$$

$$= \frac{12x^3}{4x} - \frac{36x^2}{4x} + \frac{16x}{4x}$$

$$= 3x^2 - 9x + 4$$

# Divide Polynomials by Binomials

Factor and simplify

Example:

$$(7w^2 + 3w - 4) \div (w + 1)$$

$$= \frac{7w^2 + 3w - 4}{w + 1}$$

$$= \frac{(7w - 4)(w + 1)}{w + 1}$$

$$= 7w - 4$$

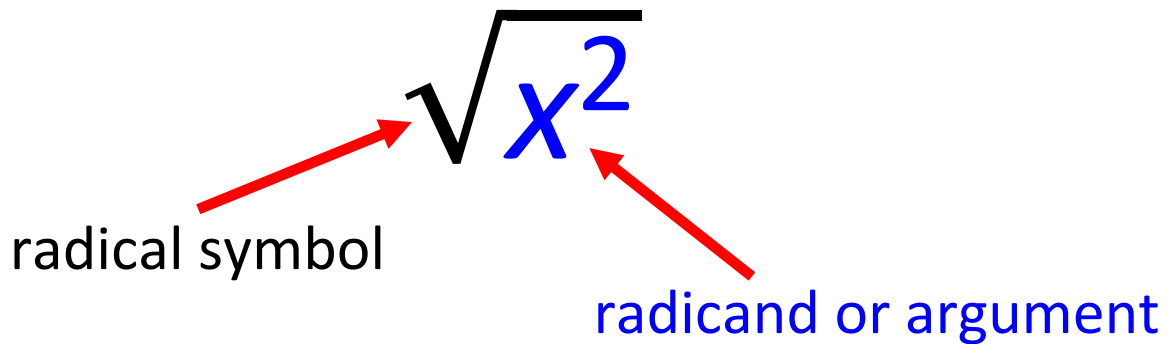
# Prime Polynomial

Cannot be factored into a product of lesser degree polynomial factors

Example
$r$
$3t + 9$
$x^2 + 1$
$5y^2 - 4y + 3$

Nonexample	Factors
$x^2 - 4$	$(x + 2)(x - 2)$
$3x^2 - 3x + 6$	$3(x + 1)(x - 2)$
$x^3$	$x \cdot x^2$

# Square Root



Simply square root expressions.

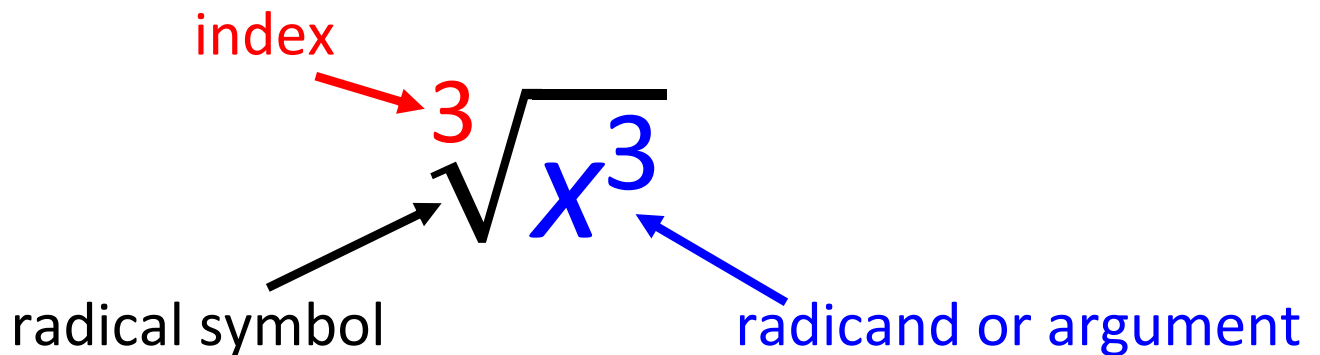
Examples:

$$\sqrt{9x^2} = \sqrt{3^2 \cdot x^2} = \sqrt{(3x)^2} = 3x$$

$$-\sqrt{(x-3)^2} = -(x-3) = -x+3$$

Squaring a number and taking a square root are inverse operations.

# Cube Root



Simplify cube root expressions.

Examples:

$$\sqrt[3]{64} = \sqrt[3]{4^3} = 4$$

$$\sqrt[3]{-27} = \sqrt[3]{(-3)^3} = -3$$

$$\sqrt[3]{x^3} = x$$

Cubing a number and taking a cube root are inverse operations.

# Product Property of Radicals

The square root of a product equals the product of the square roots of the factors.

$$\sqrt{ab} = \sqrt{a} \cdot \sqrt{b}$$

$$a \geq 0 \text{ and } b \geq 0$$

Examples:

$$\sqrt{4x} = \sqrt{4} \cdot \sqrt{x} = 2\sqrt{x}$$

$$\sqrt{5a^3} = \sqrt{5} \cdot \sqrt{a^3} = a\sqrt{5a}$$

$$\sqrt[3]{16} = \sqrt[3]{8 \cdot 2} = \sqrt[3]{8} \cdot \sqrt[3]{2} = 2\sqrt[3]{2}$$

# Quotient Property of Radicals

The square root of a quotient equals the quotient of the square roots of the numerator and denominator.

$$\sqrt{\frac{a}{b}} = \frac{\sqrt{a}}{\sqrt{b}}$$

$$a \geq 0 \text{ and } b > 0$$

Example:

$$\sqrt{\frac{5}{y^2}} = \frac{\sqrt{5}}{\sqrt{y^2}} = \frac{\sqrt{5}}{y}, y \neq 0$$



# Zero Product Property

If  $ab = 0$ ,  
then  $a = 0$  or  $b = 0$ .

Example:

$$(x + 3)(x - 4) = 0$$

$$(x + 3) = 0 \text{ or } (x - 4) = 0$$

$$x = -3 \text{ or } x = 4$$

The **solutions** are -3 and 4, also called **roots** of the equation.

# Solutions or Roots

$$x^2 + 2x = 3$$

Solve using the zero product property.

$$x^2 + 2x - 3 = 0$$

$$(x + 3)(x - 1) = 0$$

$$x + 3 = 0 \quad \text{or} \quad x - 1 = 0$$

$$x = -3 \quad \text{or} \quad x = 1$$

The **solutions** or **roots** of the polynomial equation are **-3** and **1**.

# Zeros

The **zeros** of a function  $f(x)$  are the values of  $x$  where the function is equal to zero.

$$f(x) = x^2 + 2x - 3$$

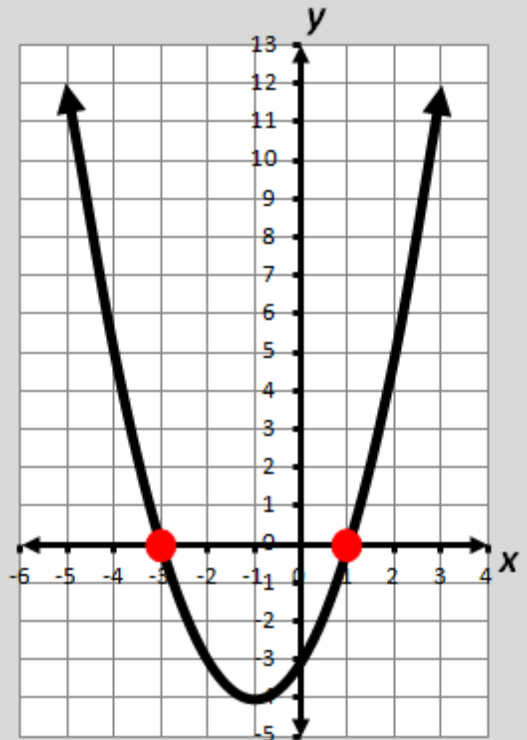
$$\text{Find } f(x) = 0.$$

$$0 = x^2 + 2x - 3$$

$$0 = (x + 3)(x - 1)$$

$$x = -3 \text{ or } x = 1$$

The **zeros** are **-3** and **1** located at **(-3,0)** and **(1,0)**.



The **zeros** of a function are also the **solutions** or **roots** of the related equation.

# x-Intercepts

The **x-intercepts** of a graph are located where the graph crosses the x-axis and where  $f(x) = 0$ .

$$f(x) = x^2 + 2x - 3$$

$$0 = (x + 3)(x - 1)$$

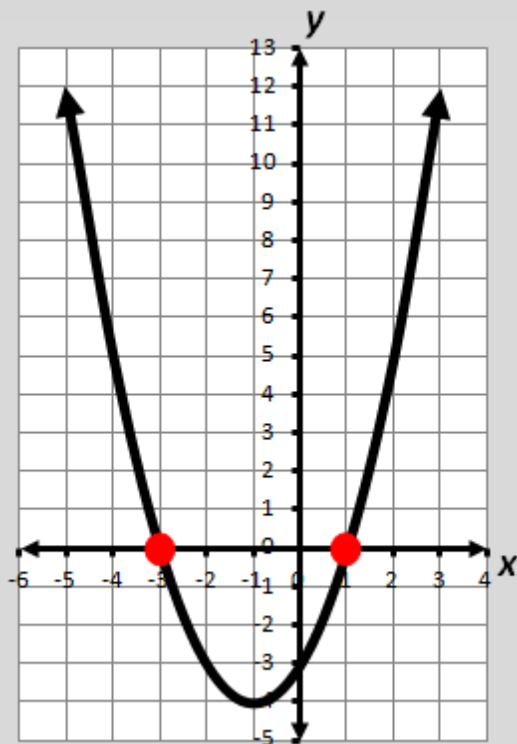
$$0 = x + 3 \text{ or } 0 = x - 1$$

$$x = -3 \text{ or } x = 1$$

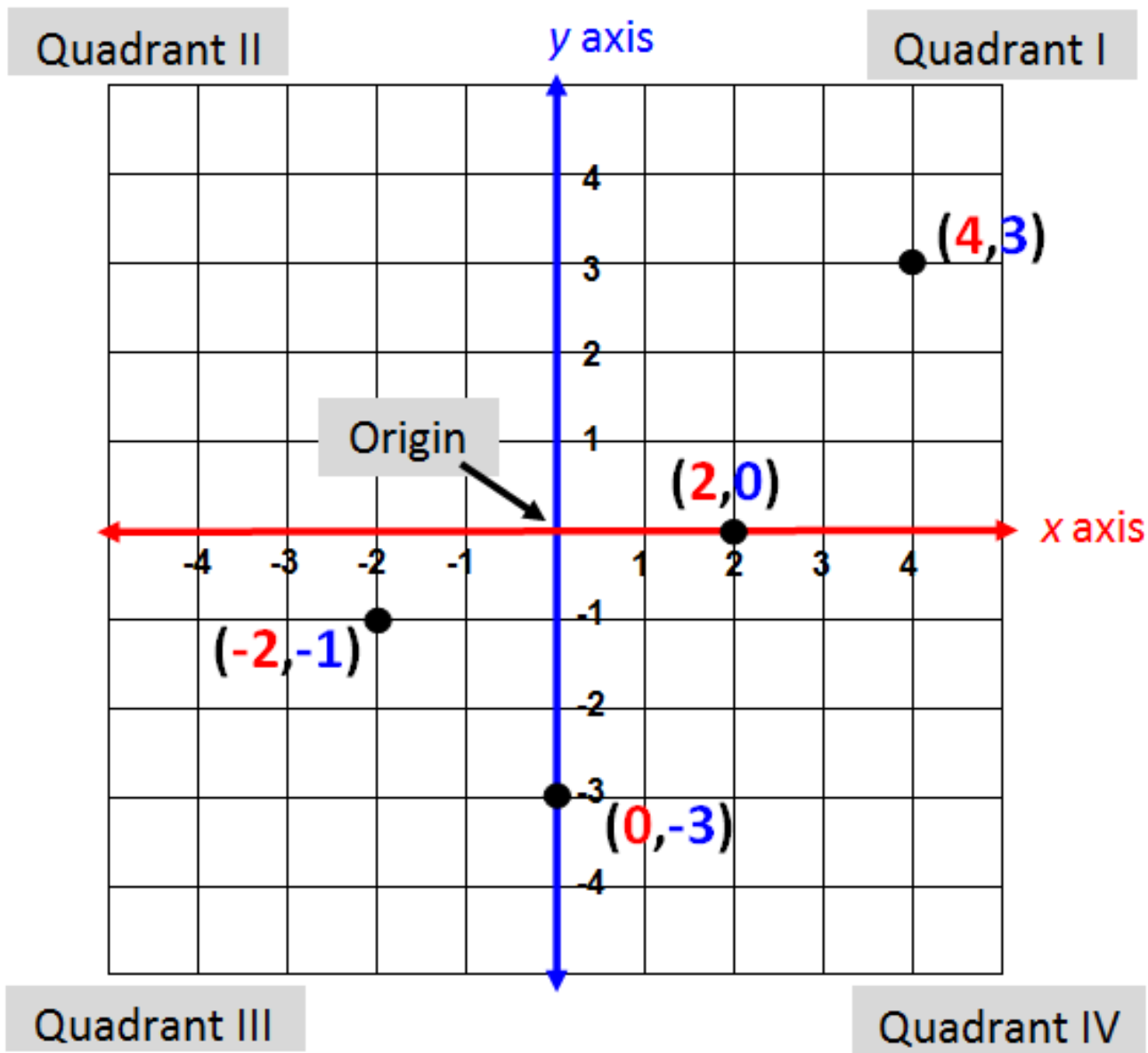
The zeros are -3 and 1.

The **x-intercepts** are:

- **-3** or **(-3,0)**
- **1** or **(1,0)**



# Coordinate Plane



ordered pair  $(x, y)$   
(abscissa, ordinate)

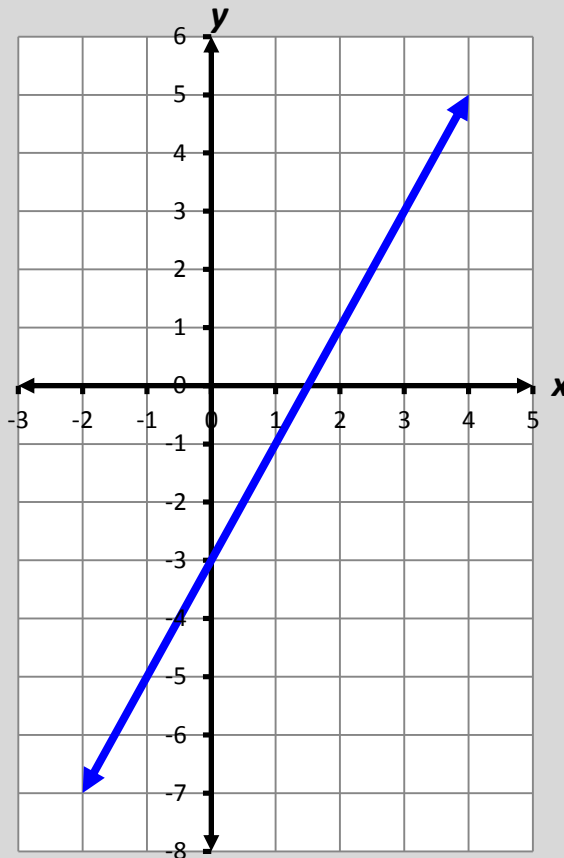
# Linear Equation

$$Ax + By = C$$

(A, B and C are integers; A and B cannot both equal zero.)

Example:

$$-2x + y = -3$$



The graph of the linear equation is a straight line and represents all solutions  $(x, y)$  of the equation.

# Linear Equation: Standard Form

$$Ax + By = C$$

(A, B, and C are integers;  
A and B cannot both equal zero.)

Examples:

$$4x + 5y = -24$$

$$x - 6y = 9$$

# Literal Equation

A formula or equation which consists primarily of variables

Examples:

$$ax + b = c$$

$$A = \frac{1}{2}bh$$

$$V = lwh$$

$$F = \frac{9}{5}C + 32$$

$$A = \pi r^2$$



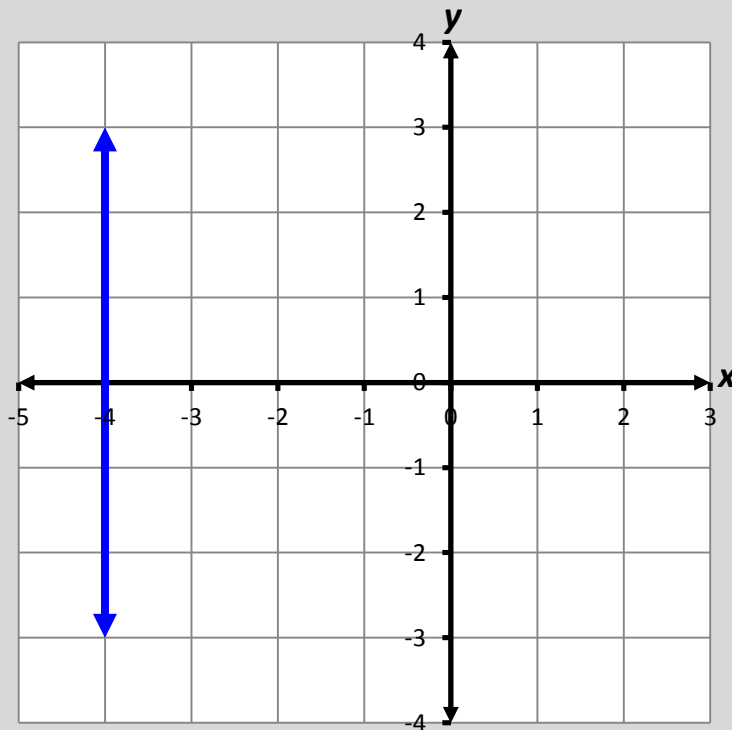
# Vertical Line

$$x = a$$

(where  $a$  can be any real number)

Example:

$$x = -4$$



Vertical lines have **an undefined slope.**

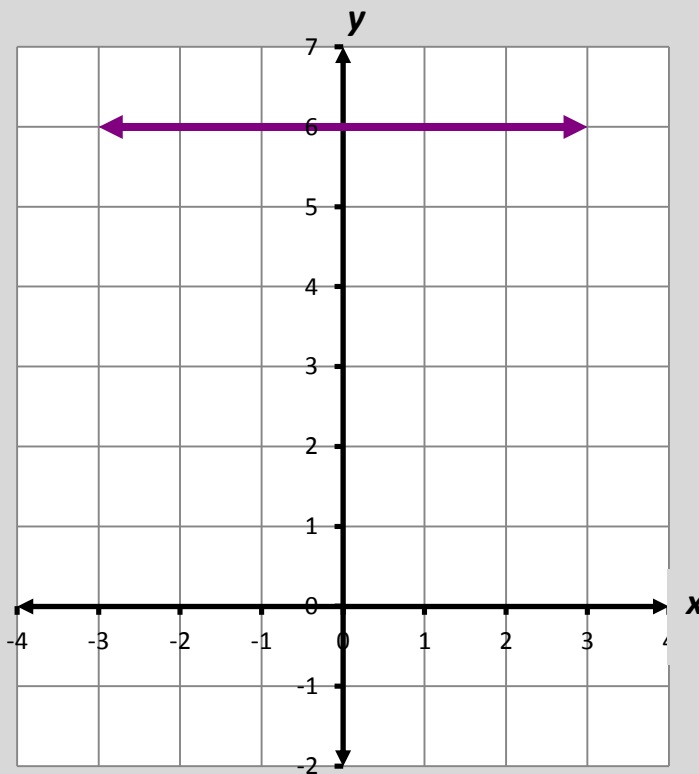
# Horizontal Line

$$y = c$$

(where  $c$  can be any real number)

Example:

$$y = 6$$



Horizontal lines have a slope of 0.

# Quadratic Equation

$$ax^2 + bx + c = 0$$

$$a \neq 0$$

Example:  $x^2 - 6x + 8 = 0$

**Solve by factoring**

$$x^2 - 6x + 8 = 0$$

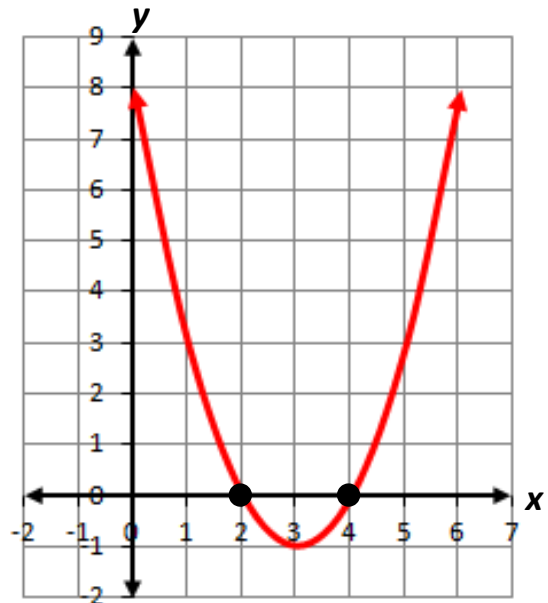
$$(x - 2)(x - 4) = 0$$

$$(x - 2) = 0 \text{ or } (x - 4) = 0$$

$$x = 2 \text{ or } x = 4$$

**Solve by graphing**

Graph the related function  $f(x) = x^2 - 6x + 8$ .



Solutions to the equation are 2 and 4;  
the  $x$ -coordinates where the curve crosses the  $x$ -axis.

# Quadratic Equation

$$ax^2 + bx + c = 0$$

$$a \neq 0$$

Example solved by factoring:

$x^2 - 6x + 8 = 0$	Quadratic equation
$(x - 2)(x - 4) = 0$	Factor
$(x - 2) = 0$ or $(x - 4) = 0$	Set factors equal to 0
$x = 2$ or $x = 4$	Solve for x

Solutions to the equation are 2 and 4.

# Quadratic Equation

$$ax^2 + bx + c = 0$$

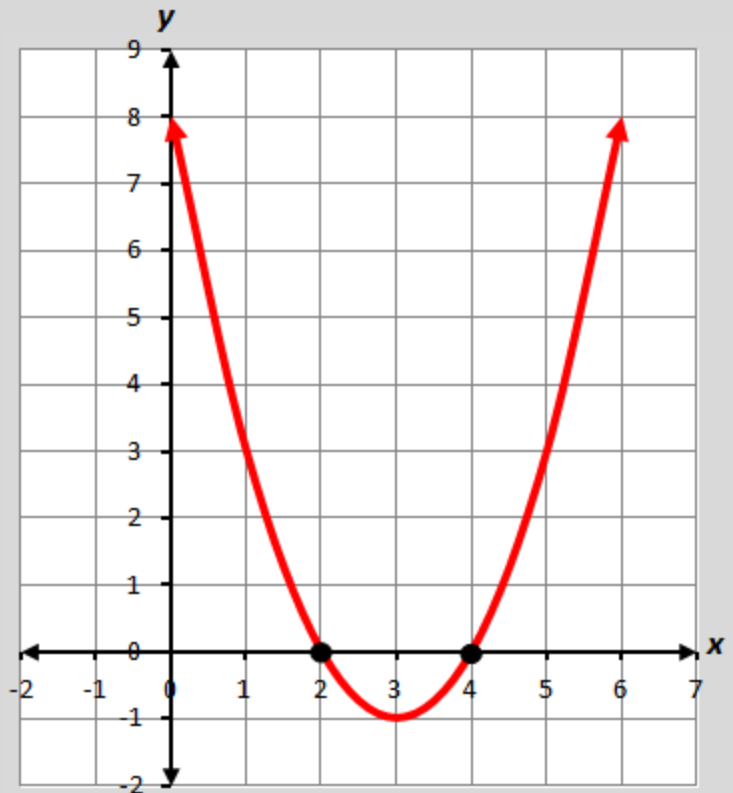
$$a \neq 0$$

Example solved by graphing:

$$x^2 - 6x + 8 = 0$$

Graph the related  
function

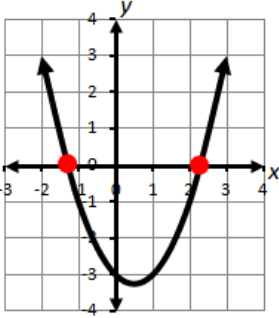
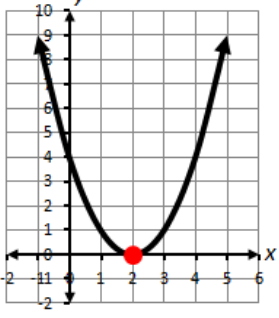
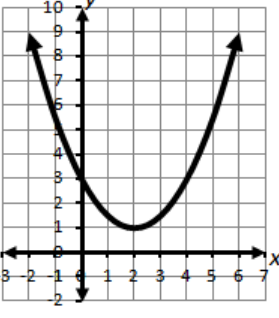
$$f(x) = x^2 - 6x + 8.$$



Solutions to the equation are the  $x$ -coordinates (2 and 4) of the points where the curve crosses the  $x$ -axis.

# Quadratic Equation: Number of Real Solutions

$$ax^2 + bx + c = 0, a \neq 0$$

Examples	Graphs	Number of Real Solutions/Roots
$x^2 - x = 3$		2
$x^2 + 16 = 8x$		1 distinct root with a multiplicity of two
$2x^2 - 2x + 3 = 0$		0

# Identity Property of Addition

$$a + 0 = 0 + a = a$$

Examples:

$$3.8 + 0 = 3.8$$

$$6x + 0 = 6x$$

$$0 + (-7 + r) = -7 + r$$

Zero is the additive identity.

# Inverse Property of Addition

$$a + (-a) = (-a) + a = 0$$

Examples:

$$4 + (-4) = 0$$

$$0 = (-9.5) + 9.5$$

$$x + (-x) = 0$$

$$0 = 3y + (-3y)$$



# Commutative Property of Addition

$$a + b = b + a$$

Examples:

$$2.76 + 3 = 3 + 2.76$$

$$x + 5 = 5 + x$$

$$(a + 5) - 7 = (5 + a) - 7$$

$$11 + (b - 4) = (b - 4) + 11$$

# Associative Property of Addition

$$(a + b) + c = a + (b + c)$$

Examples:

$$\left(5 + \frac{3}{5}\right) + \frac{1}{10} = 5 + \left(\frac{3}{5} + \frac{1}{10}\right)$$

$$3x + (2x + 6y) = (3x + 2x) + 6y$$

# Identity Property of Multiplication

$$a \cdot 1 = 1 \cdot a = a$$

Examples:

$$3.8 (1) = 3.8$$

$$6x \cdot 1 = 6x$$

$$1(-7) = -7$$

One is the multiplicative identity.

# Inverse Property of Multiplication

$$a \cdot \frac{1}{a} = \frac{1}{a} \cdot a = 1$$

$a \neq 0$

Examples:

$$7 \cdot \frac{1}{7} = 1$$

$$\frac{5}{x} \cdot \frac{x}{5} = 1, x \neq 0$$

$$\frac{-1}{3} \cdot (-3p) = 1p = p$$

The multiplicative inverse of  $a$  is  $\frac{1}{a}$ .

# Commutative Property of Multiplication

$$ab = ba$$

Examples:

$$(-8)\left(\frac{2}{3}\right) = \left(\frac{2}{3}\right)(-8)$$

$$y \cdot 9 = 9 \cdot y$$

$$4(2x \cdot 3) = 4(3 \cdot 2x)$$

$$8 + 5x = 8 + x \cdot 5$$

# Associative Property of Multiplication

$$(ab)c = a(bc)$$

Examples:

$$(1 \cdot 8) \cdot 3\frac{3}{4} = 1 \cdot (8 \cdot 3\frac{3}{4})$$

$$(3x)x = 3(x \cdot x)$$

# Distributive Property

$$a(b + c) = ab + ac$$

Examples:

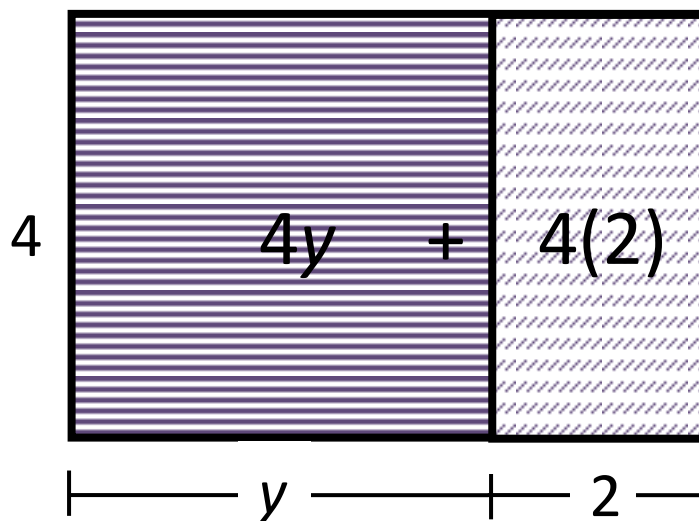
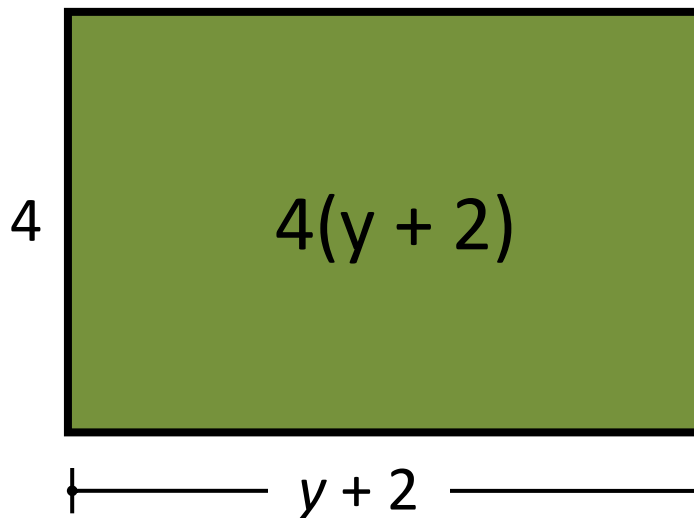
$$5\left(y - \frac{1}{3}\right) = (5 \cdot y) - \left(5 \cdot \frac{1}{3}\right)$$

$$2 \cdot x + 2 \cdot 5 = 2(x + 5)$$

$$3.1a + (1)(a) = (3.1 + 1)a$$

# Distributive Property

$$4(y + 2) = 4y + 4(2)$$





# Multiplicative Property of Zero

$$a \cdot 0 = 0 \text{ or } 0 \cdot a = 0$$

Examples:

$$8\frac{2}{3} \cdot 0 = 0$$

$$0 \cdot (-13y - 4) = 0$$

# Substitution Property

If  $a = b$ , then  $b$  can replace  $a$  in a given equation or inequality.

Examples:

Given	Given	Substitution
$r = 9$	$3r = 27$	$3(9) = 27$
$b = 5a$	$24 < b + 8$	$24 < 5a + 8$
$y = 2x + 1$	$2y = 3x - 2$	$2(2x + 1) = 3x - 2$

# Reflexive Property of Equality

$$a = a$$

$a$  is any real number

Examples:

$$-4 = -4$$

$$3.4 = 3.4$$

$$9y = 9y$$

# Symmetric Property of Equality

If  $a = b$ , then  $b = a$ .

Examples:

If  $12 = r$ , then  $r = 12$ .

If  $-14 = z + 9$ , then  $z + 9 = -14$ .

If  $2.7 + y = x$ , then  $x = 2.7 + y$ .

# Transitive Property of Equality

If  $a = b$  and  $b = c$ ,  
then  $a = c$ .

Examples:

If  $4x = 2y$  and  $2y = 16$ ,  
then  $4x = 16$ .

If  $x = y - 1$  and  $y - 1 = -3$ ,  
then  $x = -3$ .

# Inequality

An algebraic sentence comparing two quantities

Symbol	Meaning
$<$	less than
$\leq$	less than or equal to
$>$	greater than
$\geq$	greater than or equal to
$\neq$	not equal to

Examples:




$$-10.5 > -9.9 - 1.2$$

$$8 > 3t + 2$$

$$x - 5y \geq -12$$

$$r \neq 3$$

# Graph of an Inequality

Symbol	Examples	Graph
$<$ or $>$	$x < 3$	 A number line with arrows at both ends, labeled from -1 to 5. A red circle with a plus sign is drawn at the number 3. A red line with arrows at both ends extends from the circle to the left, passing through 2, 1, 0, and -1.
$\leq$ or $\geq$	$-3 \geq y$	 A number line with arrows at both ends, labeled from -6 to 0. A red circle with a plus sign is drawn at the number -3. A red line with arrows at both ends extends from the circle to the left, passing through -4, -5, and -6.
$\neq$	$t \neq -2$	 A number line with arrows at both ends, labeled from -6 to 0. A red circle with a plus sign is drawn at the number -2. A red line with arrows at both ends extends from the circle to the left, passing through -3, -4, -5, and -6.

# Transitive Property of Inequality

If	Then
$a < b$ and $b < c$	$a < c$
$a > b$ and $b > c$	$a > c$

Examples:

If  $4x < 2y$  and  $2y < 16$ ,  
then  $4x < 16$ .

If  $x > y - 1$  and  $y - 1 > 3$ ,  
then  $x > 3$ .



# Addition/Subtraction Property of Inequality

If	Then
$a > b$	$a + c > b + c$
$a \geq b$	$a + c \geq b + c$
$a < b$	$a + c < b + c$
$a \leq b$	$a + c \leq b + c$

Example:

$$d - 1.9 \geq -8.7$$

$$d - 1.9 + 1.9 \geq -8.7 + 1.9$$

$$d \geq -6.8$$

# Multiplication Property of Inequality

If	Case	Then
$a < b$	$c > 0$ , positive	$ac < bc$
$a > b$	$c > 0$ , positive	$ac > bc$
$a < b$	$c < 0$ , negative	$ac > bc$
$a > b$	$c < 0$ , negative	$ac < bc$

Example: if  $c = -2$

$$5 > -3$$

$$5(-2) < -3(-2)$$

$$-10 < 6$$

# Division Property of Inequality

If	Case	Then
$a < b$	$c > 0$ , positive	$\frac{a}{c} < \frac{b}{c}$
$a > b$	$c > 0$ , positive	$\frac{a}{c} > \frac{b}{c}$
$a < b$	$c < 0$ , negative	$\frac{a}{c} > \frac{b}{c}$
$a > b$	$c < 0$ , negative	$\frac{a}{c} < \frac{b}{c}$

Example: if  $c = -4$

$$-90 \geq -4t$$

$$\frac{-90}{-4} \leq \frac{-4t}{-4}$$

$$22.5 \leq t$$

# Linear Equation: Slope-Intercept Form

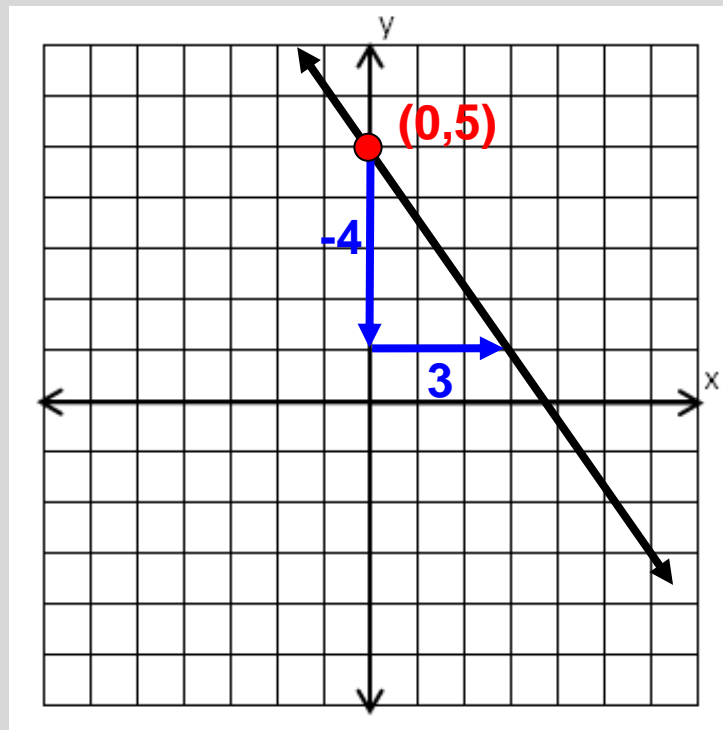
$$y = mx + b$$

(slope is  $m$  and  $y$ -intercept is  $b$ )

Example:  $y = \frac{-4}{3}x + 5$

$$m = \frac{-4}{3}$$

$$b = 5$$



# Linear Equation: Point-Slope Form

$$y - y_1 = m(x - x_1)$$

where  $m$  is the slope and  $(x_1, y_1)$  is the point

Example:

Write an equation for the line that passes through the point  $(-4, 1)$  and has a slope of 2.

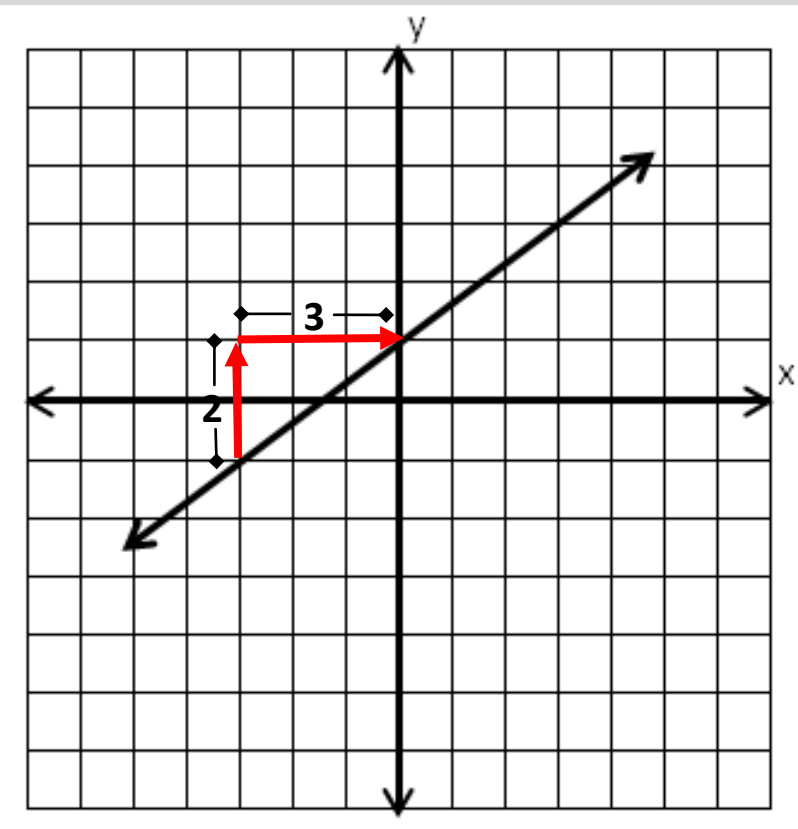
$$y - 1 = 2(x - -4)$$

$$y - 1 = 2(x + 4)$$

$$y = 2x + 9$$

# Slope

A number that represents the rate of change in  $y$  for a unit change in  $x$

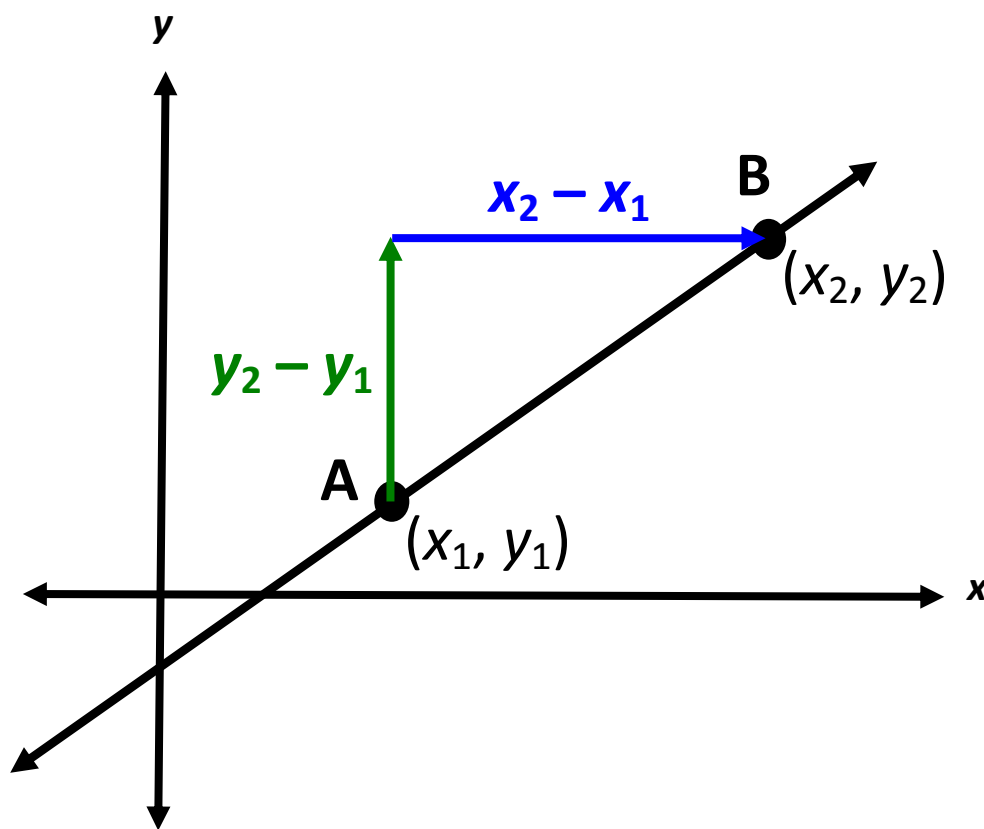


$$\text{Slope} = \frac{2}{3}$$

The slope indicates the steepness of a line.

# Slope Formula

The ratio of vertical change to horizontal change

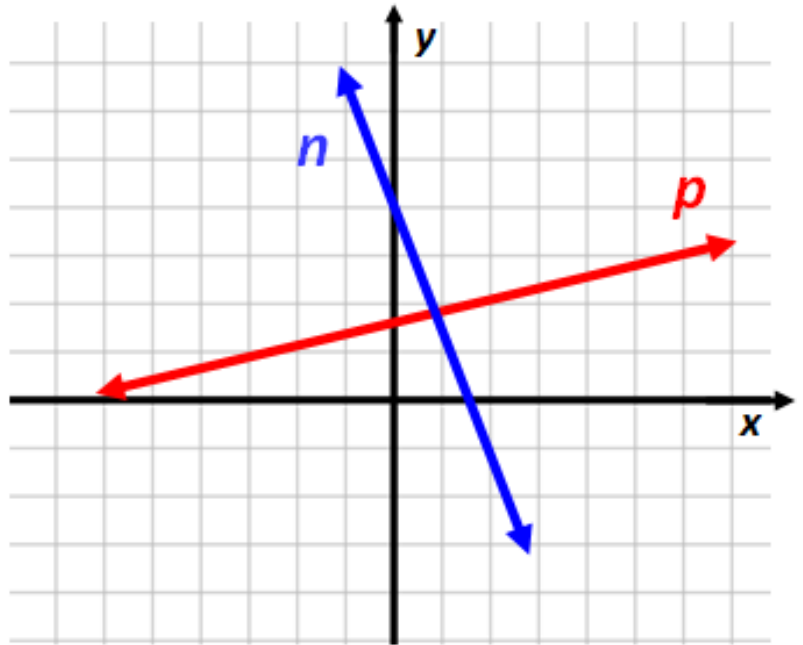


$$\text{slope} = m = \frac{\text{change in } y}{\text{change in } x} = \frac{y_2 - y_1}{x_2 - x_1}$$

# Slopes of Lines

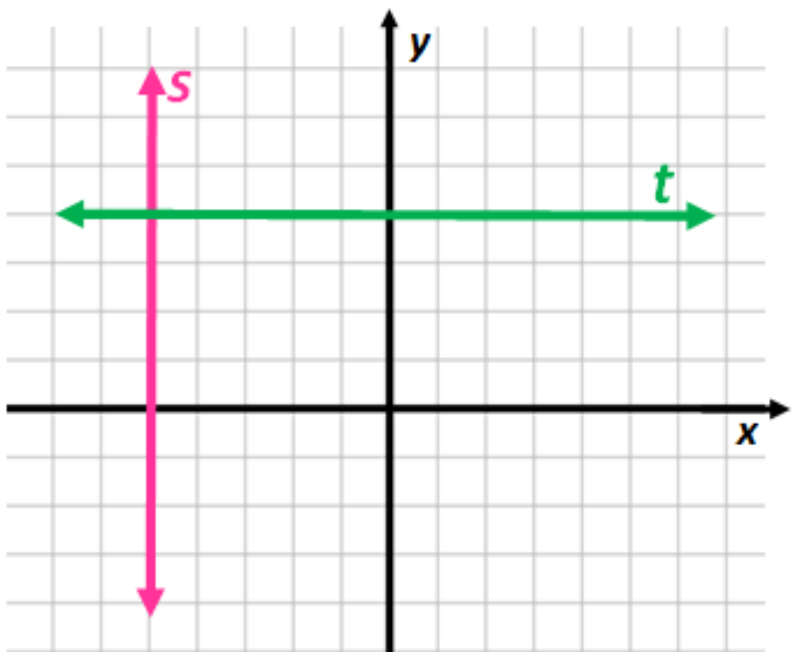
Line  $p$   
has a positive  
slope.

Line  $n$   
has a negative  
slope.



Vertical line  $s$  has  
an undefined  
slope.

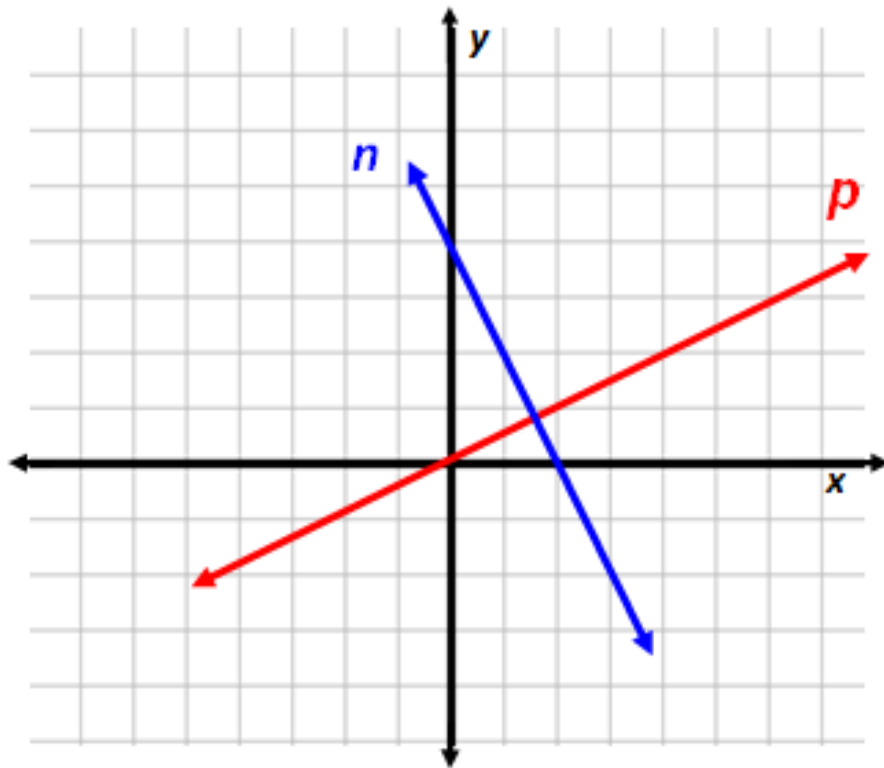
Horizontal line  $t$   
has a zero slope.





# Perpendicular Lines

Lines that intersect to form a right angle



Perpendicular lines (not parallel to either of the axes) have slopes whose product is  $-1$ .

Example:

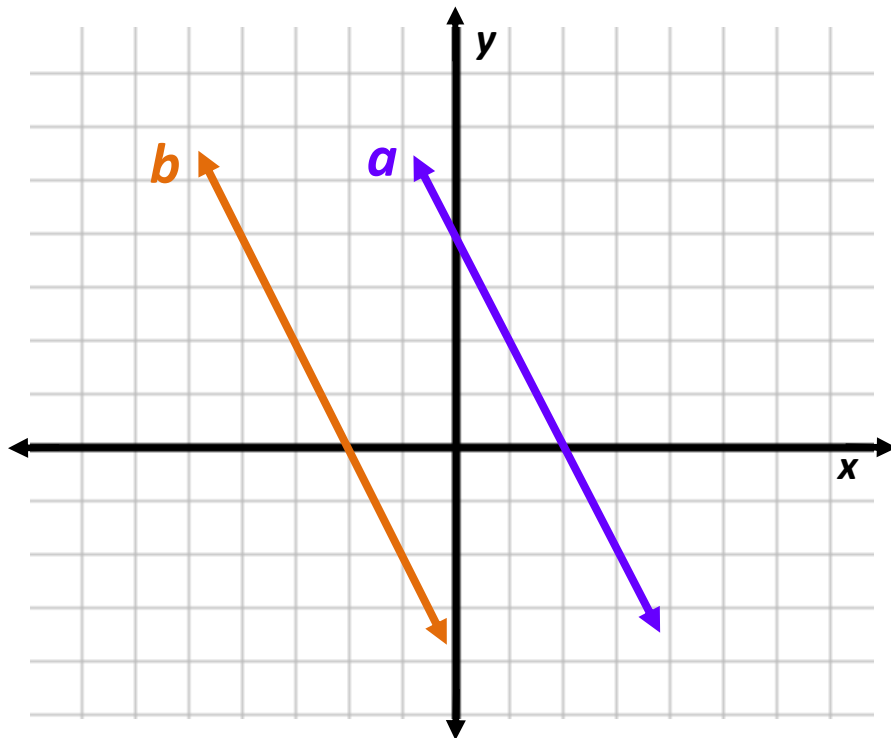
The slope of line  $n = -2$ . The slope of line  $p = \frac{1}{2}$ .

$-2 \cdot \frac{1}{2} = -1$ , therefore,  $n$  is perpendicular to  $p$ .

# Parallel Lines

Lines in the same plane that do not intersect are parallel.

Parallel lines have the same slopes.



Example:

The slope of line  $a = -2$ .

The slope of line  $b = -2$ .

$-2 = -2$ , therefore,  $a$  is parallel to  $b$ .

# Mathematical Notation

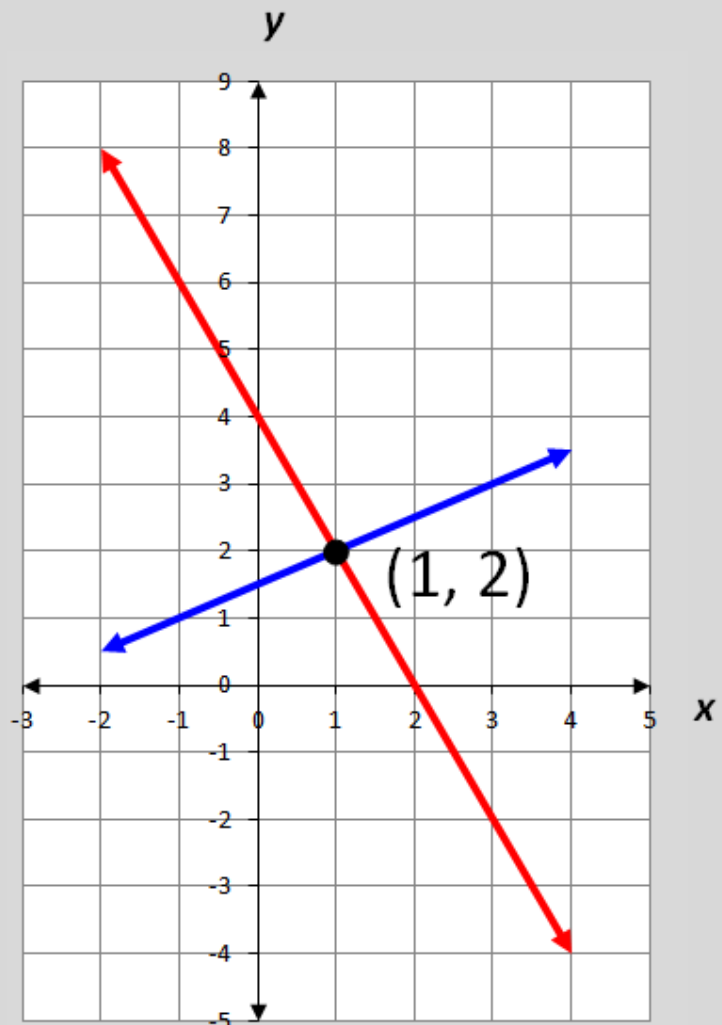
Set Builder Notation	Read	Other Notation
$\{x \mid 0 < x \leq 3\}$	The set of all $x$ such that $x$ is greater than or equal to 0 and $x$ is less than 3.	$0 < x \leq 3$ $(0, 3]$
$\{y: y \geq -5\}$	The set of all $y$ such that $y$ is greater than or equal to -5.	$y \geq -5$ $[-5, \infty)$

# System of Linear Equations

Solve by graphing:

$$\begin{cases} -x + 2y = 3 \\ 2x + y = 4 \end{cases}$$

The solution,  $(1, 2)$ , is the only ordered pair that satisfies both equations (the point of intersection).



# System of Linear Equations

Solve by substitution:

$$\begin{cases} x + 4y = 17 \\ y = x - 2 \end{cases}$$

Substitute  $x - 2$  for  $y$  in the first equation.

$$x + 4(x - 2) = 17$$

$$x = 5$$

Now substitute  $5$  for  $x$  in the second equation.

$$y = 5 - 2$$

$$y = 3$$

The solution to the linear system is  $(5, 3)$ , the ordered pair that satisfies both equations.

# System of Linear Equations

Solve by elimination:

$$\begin{cases} -5x - 6y = 8 \\ 5x + 2y = 4 \end{cases}$$

Add or subtract the equations to eliminate one variable.

$$\begin{array}{r} -5x - 6y = 8 \\ + 5x + 2y = 4 \\ \hline -4y = 12 \\ y = -3 \end{array}$$

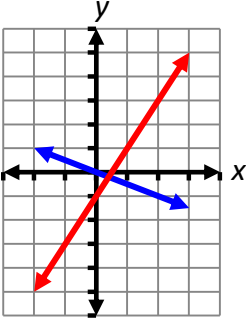
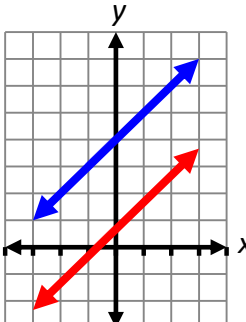
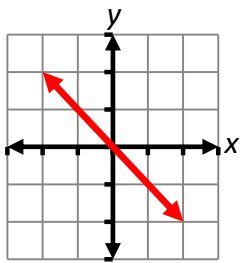
Now substitute -3 for y in either original equation to find the value of x, the eliminated variable.

$$\begin{array}{r} -5x - 6(-3) = 8 \\ x = 2 \end{array}$$

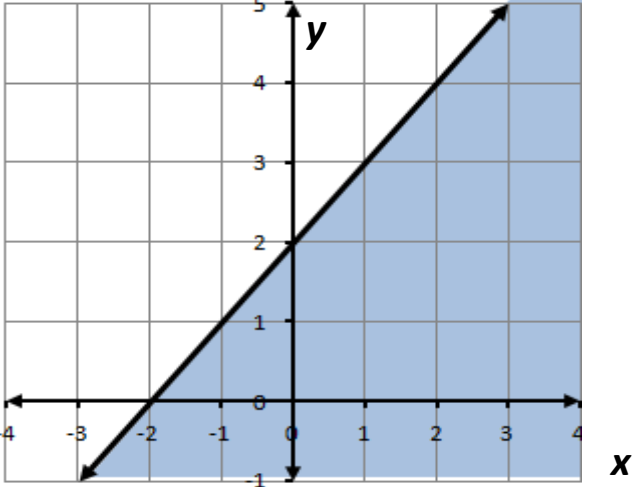
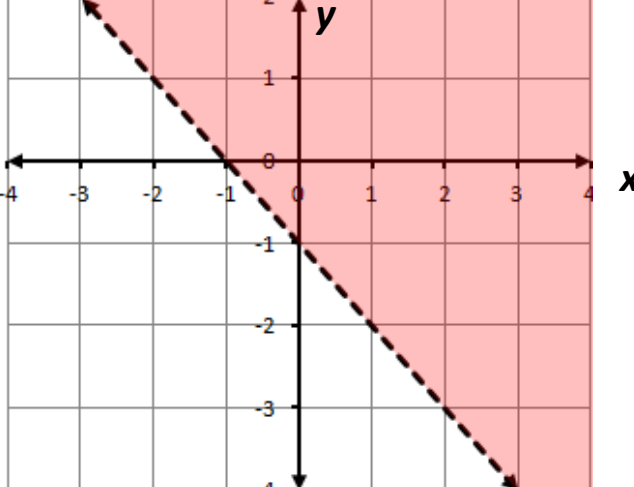
The solution to the linear system is (2,-3), the ordered pair that satisfies both equations.

# System of Linear Equations

## Identifying the Number of Solutions

Number of Solutions	Slopes and y-intercepts	Graph
One solution	Different slopes	 A coordinate plane with x and y axes. Two lines are plotted: a red line with a positive slope and a blue line with a negative slope. The two lines intersect at a single point in the first quadrant.
No solution	Same slope and different y-intercepts	 A coordinate plane with x and y axes. Two parallel lines are plotted, both with a positive slope. One line is blue and the other is red. They do not intersect.
Infinitely many solutions	Same slope and same y-intercepts	 A coordinate plane with x and y axes. A single red line is plotted with a negative slope, passing through the origin. This represents two overlapping lines.

# Graphing Linear Inequalities

Example	Graph
$y \leq x + 2$	
$y > -x - 1$	



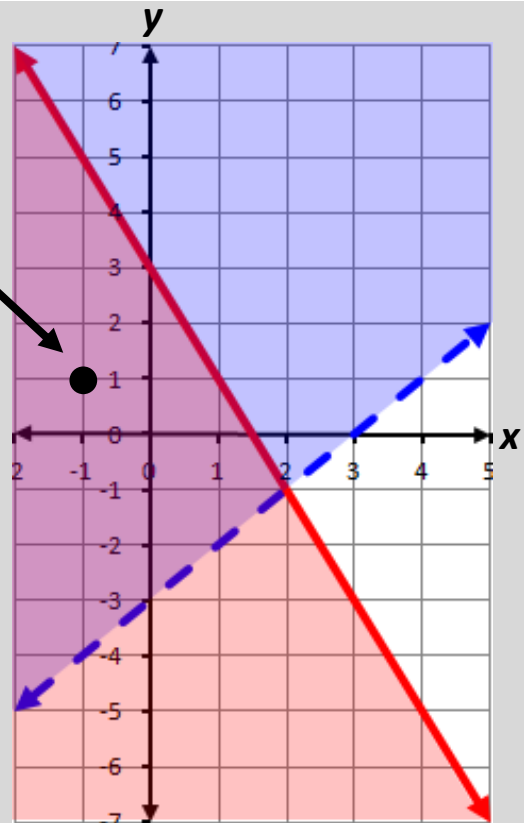
# System of Linear Inequalities

Solve by graphing:

$$\begin{cases} y > x - 3 \\ y \leq -2x + 3 \end{cases}$$

The solution region contains all ordered pairs that are solutions to both inequalities in the system.

$(-1, 1)$  is one solution to the system located in the solution region.



# Dependent and Independent Variable

$x$ , independent variable  
(input values or domain set)

Example:

$$y = 2x + 7$$

$y$ , dependent variable  
(output values or range set)

# Dependent and Independent Variable

Determine the **distance** a car will travel going 55 mph.

$$d = 55h$$

independent

$h$	$d$
0	0
1	55
2	110
3	165

dependent

# Graph of a Quadratic Equation

$$y = ax^2 + bx + c$$

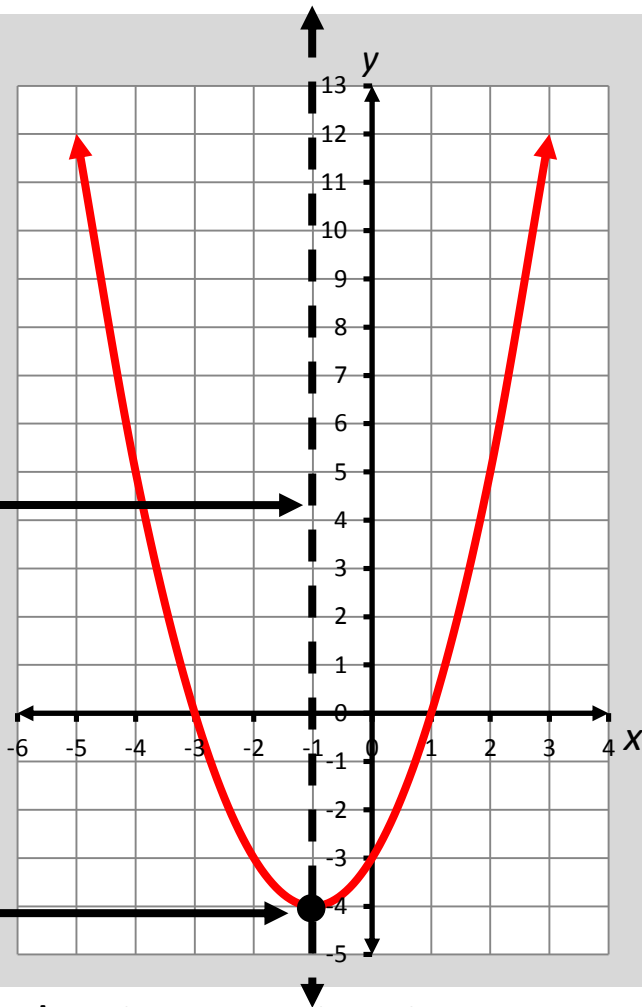
$$a \neq 0$$

Example:

$$y = x^2 + 2x - 3$$

line of symmetry

vertex



The graph of the quadratic equation is a curve (parabola) with one line of symmetry and one vertex.

# Quadratic Formula

Used to find the solutions to any quadratic equation of the form,  $y = ax^2 + bx + c$

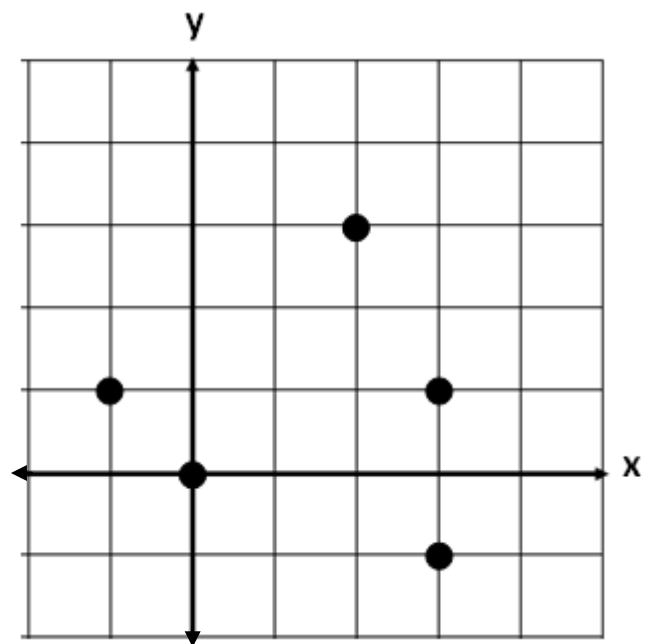
$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

# Relations

## Representations of relationships

$x$	$y$
-3	4
0	0
1	-6
2	2
5	-1

Example 1



Example 2

$\{(0,4), (0,3), (0,2), (0,1)\}$

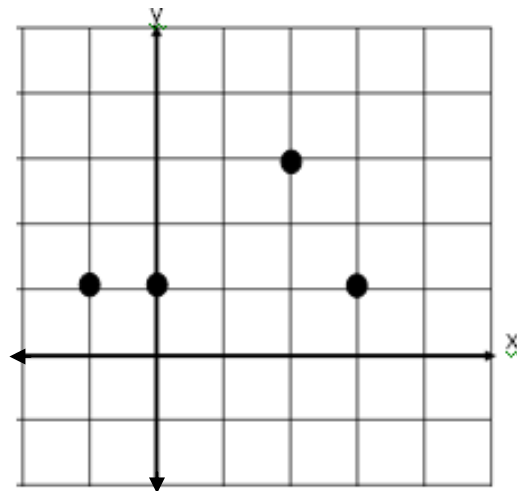
Example 3

# Functions

## Representations of functions

$x$	$y$
3	2
2	4
0	2
-1	2

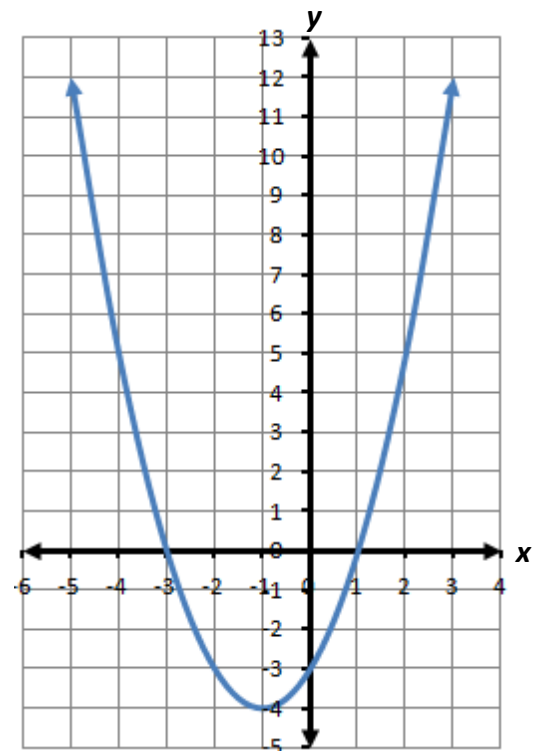
Example 1



Example 2

$\{(-3,4), (0,3), (1,2), (4,6)\}$

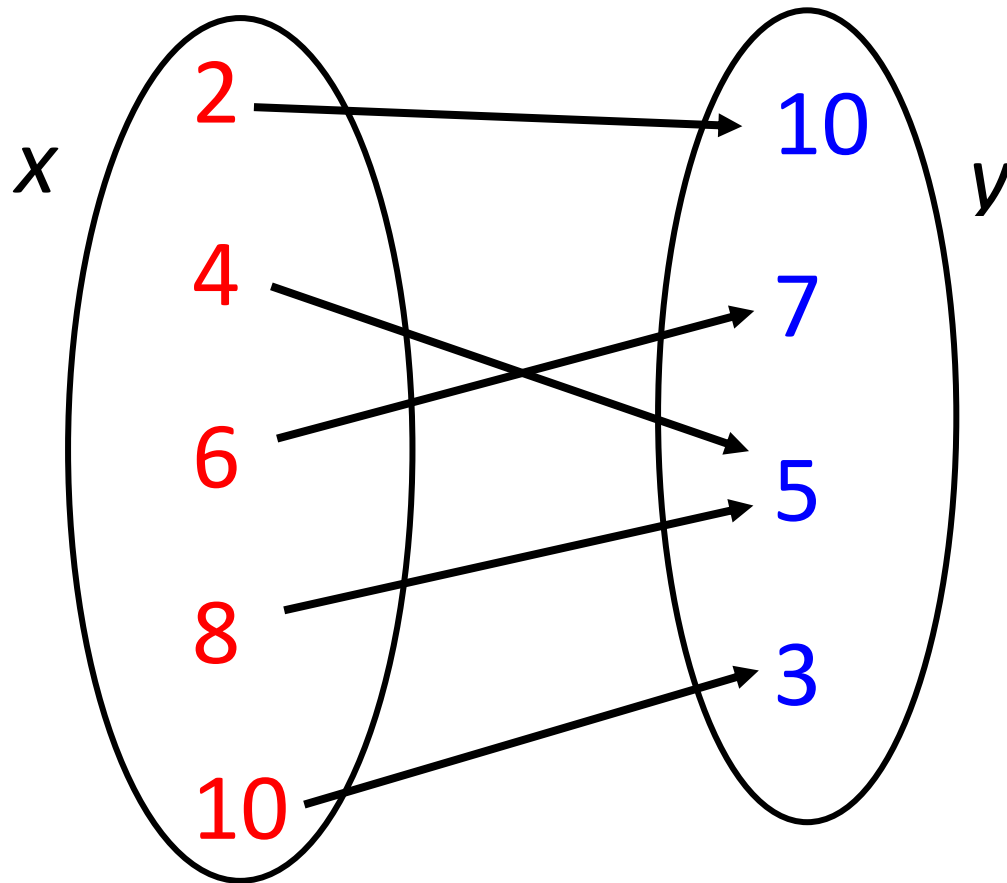
Example 3



Example 4

# Function

A relationship between two quantities in which every **input** corresponds to exactly one **output**



A relation is a function if and only if each element in the domain is paired with a unique element of the range.



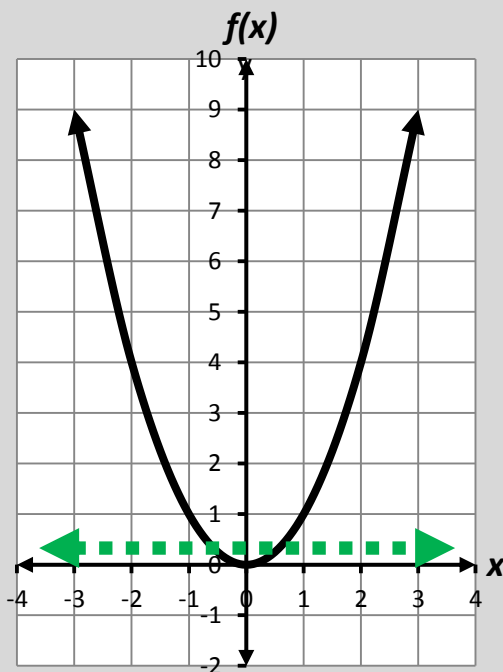
# Domain

A set of input values of a relation

Examples:

input	output
$x$	$g(x)$
-2	0
-1	1
0	2
1	3

The **domain** of  $g(x)$  is  $\{-2, -1, 0, 1\}$ .



The **domain** of  $f(x)$  is **all real numbers**.

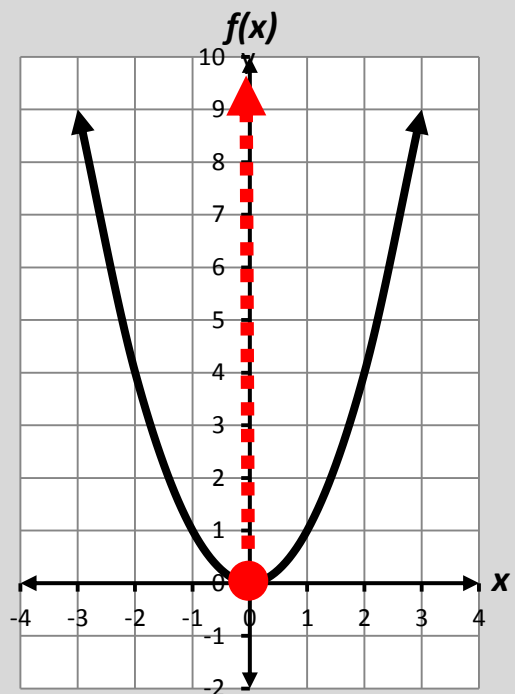
# Range

A set of output values of a relation

Examples:

input	output
$x$	$g(x)$
-2	0
-1	1
0	2
1	3

The **range** of  $g(x)$  is  $\{0, 1, 2, 3\}$ .



The **range** of  $f(x)$  is **all real numbers greater than or equal to zero.**

# Function Notation

$$f(x)$$

$f(x)$  is read  
“the value of  $f$  at  $x$ ” or “ $f$  of  $x$ ”

Example:

$$f(x) = -3x + 5, \text{ find } f(2).$$

$$f(2) = -3(2) + 5$$

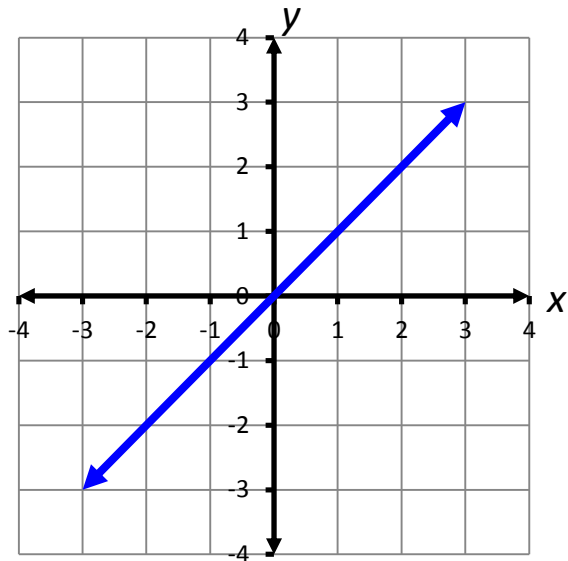
$$f(2) = -6$$

Letters other than  $f$  can be used to name functions, e.g.,  $g(x)$  and  $h(x)$

# Parent Functions

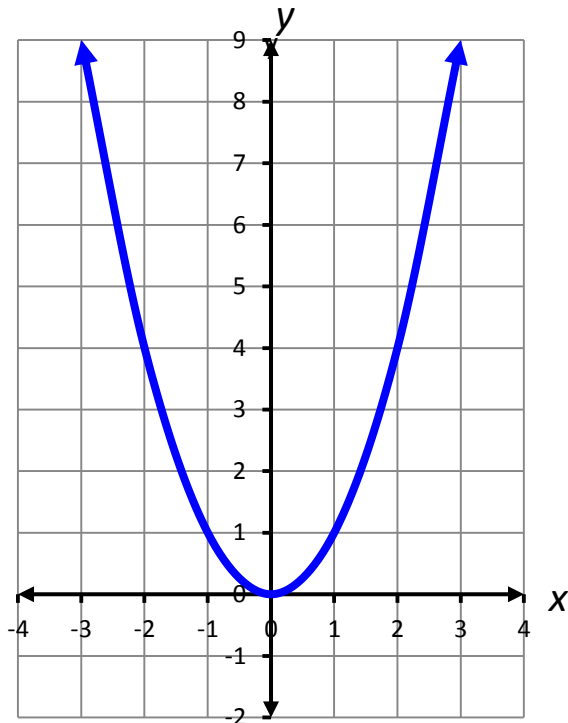
Linear

$$f(x) = x$$



Quadratic

$$f(x) = x^2$$



# Transformations of Parent Functions

Parent functions can be transformed to create other members in a family of graphs.

<b>Translations</b>	$g(x) = f(x) + k$ is the graph of $f(x)$ translated vertically –	$k$ units <b>up</b> when $k > 0$ .
		$k$ units <b>down</b> when $k < 0$ .
	$g(x) = f(x - h)$ is the graph of $f(x)$ translated horizontally –	$h$ units <b>right</b> when $h > 0$ .
		$h$ units <b>left</b> when $h < 0$ .

# Transformations of Parent Functions

Parent functions can be transformed to create other members in a family of graphs.

<b>Reflections</b>	$g(x) = -f(x)$ is the graph of $f(x)$ –	reflected over the <b>x-axis</b> .
	$g(x) = f(-x)$ is the graph of $f(x)$ –	reflected over the <b>y-axis</b> .

# Transformations of Parent Functions

Parent functions can be transformed to create other members in a family of graphs.

<b>Dilations</b>	$g(x) = a \cdot f(x)$ is the graph of $f(x)$ –	<b>vertical dilation</b> (stretch) if $a > 1$ .
		<b>vertical dilation</b> (compression) if $0 < a < 1$ .
	$g(x) = f(ax)$ is the graph of $f(x)$ –	<b>horizontal dilation</b> (compression) if $a > 1$ .
		<b>horizontal dilation</b> (stretch) if $0 < a < 1$ .

# Transformational Graphing

Linear functions

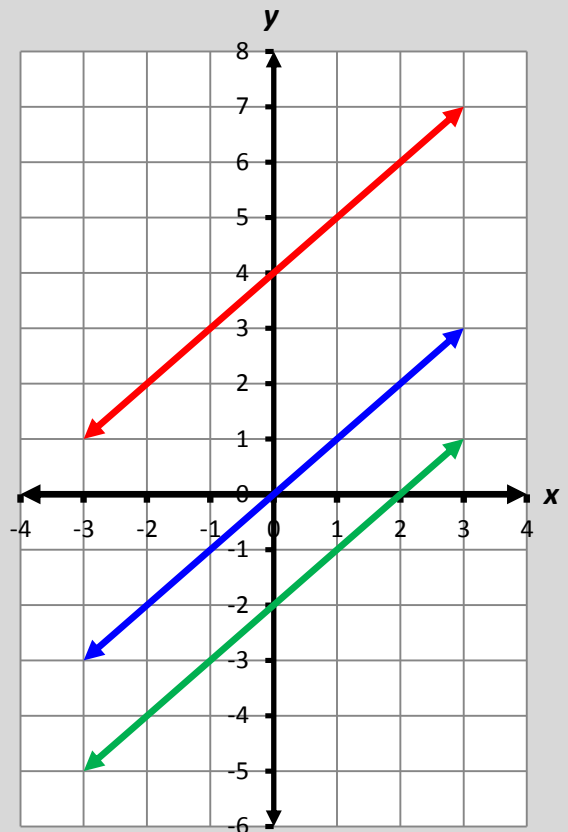
$$g(x) = x + b$$

Examples:

$$f(x) = x$$

$$t(x) = x + 4$$

$$h(x) = x - 2$$



Vertical translation of the parent  
function,  $f(x) = x$



# Transformational Graphing

Linear functions

$$g(x) = mx$$

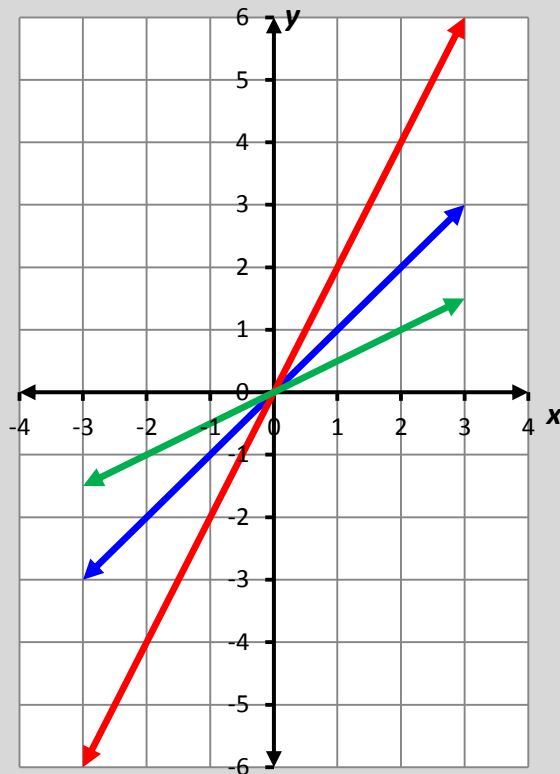
$$m > 0$$

Examples:

$$f(x) = x$$

$$t(x) = 2x$$

$$h(x) = \frac{1}{2}x$$



Vertical dilation (**stretch** or **compression**)  
of the parent function,  $f(x) = x$

# Transformational Graphing

Linear functions

$$g(x) = mx$$

$$m < 0$$

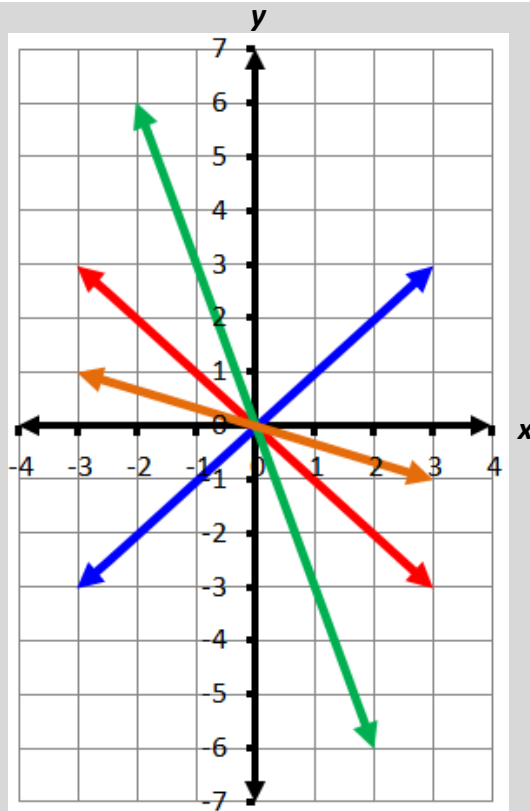
Examples:

$$f(x) = x$$

$$t(x) = -x$$

$$h(x) = -3x$$

$$d(x) = -\frac{1}{3}x$$



Vertical dilation (**stretch** or **compression**) with a **reflection** of  $f(x) = x$

# Transformational Graphing

Quadratic functions

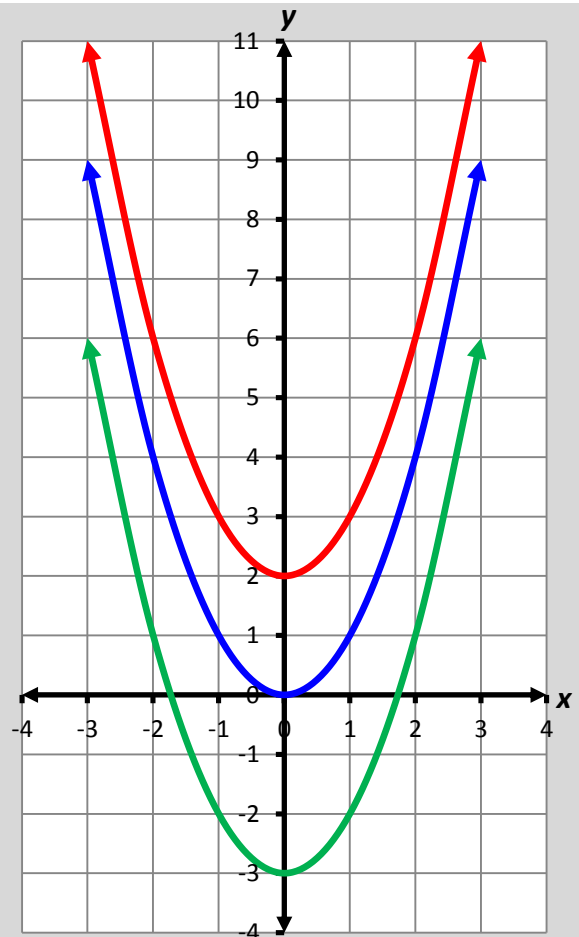
$$h(x) = x^2 + c$$

Examples:

$$f(x) = x^2$$

$$g(x) = x^2 + 2$$

$$t(x) = x^2 - 3$$



Vertical translation of  $f(x) = x^2$

# Transformational Graphing

Quadratic functions

$$h(x) = ax^2$$

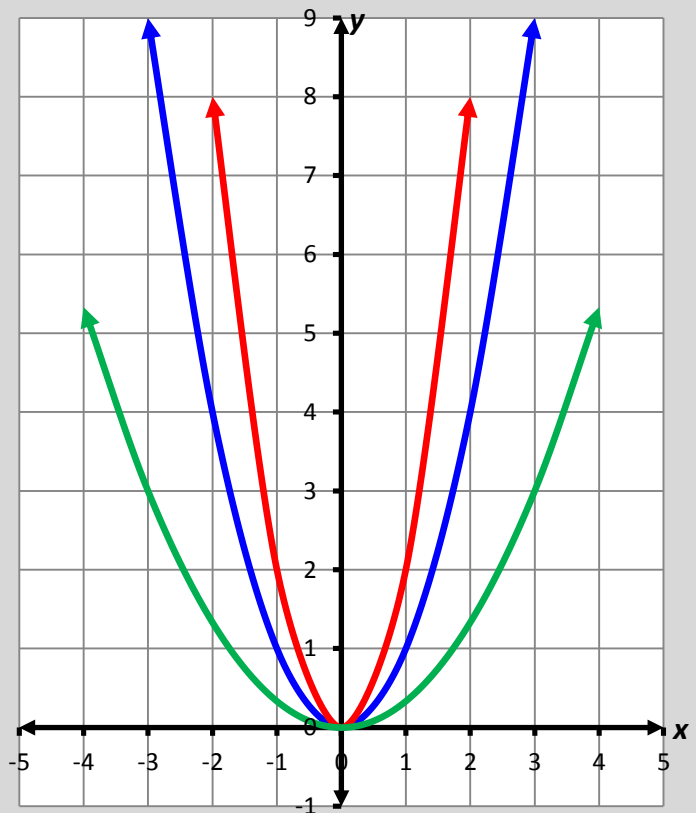
$$a > 0$$

Examples:

$$f(x) = x^2$$

$$g(x) = 2x^2$$

$$t(x) = \frac{1}{3}x^2$$



Vertical dilation (**stretch** or  
**compression**) of  $f(x) = x^2$

# Transformational Graphing

Quadratic functions

$$h(x) = ax^2$$

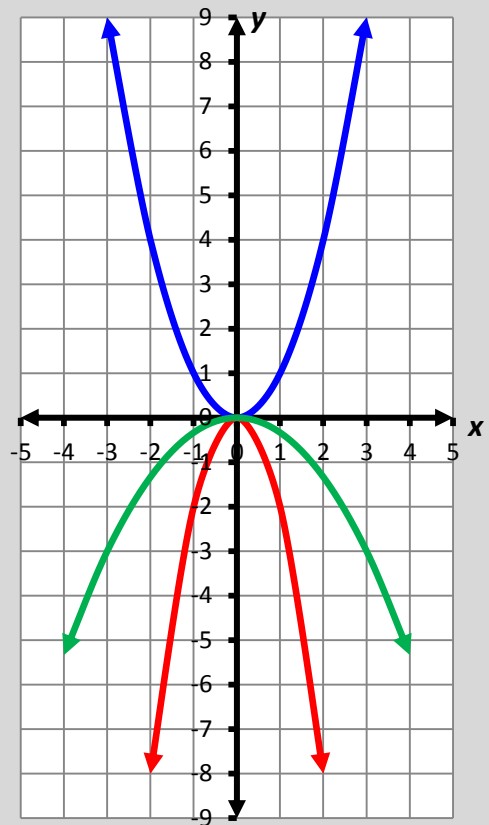
$$a < 0$$

Examples:

$$f(x) = x^2$$

$$g(x) = -2x^2$$

$$t(x) = -\frac{1}{3}x^2$$



Vertical dilation (**stretch** or **compression**)  
with a reflection of  $f(x) = x^2$

# Transformational Graphing

Quadratic functions

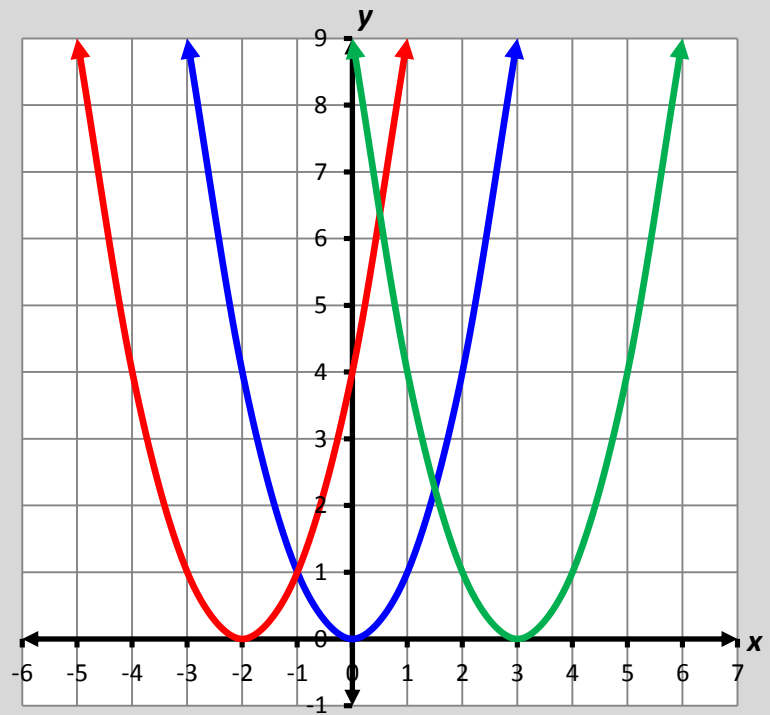
$$h(x) = (x + c)^2$$

Examples:

$$f(x) = x^2$$

$$g(x) = (x + 2)^2$$

$$t(x) = (x - 3)^2$$



Horizontal translation of  $f(x) = x^2$

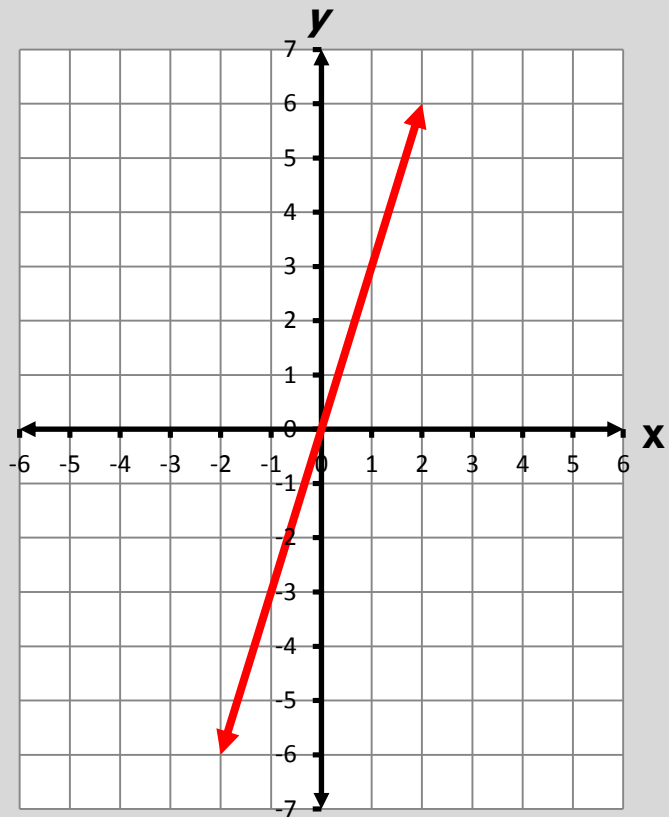
# Direct Variation

$$y = kx \text{ or } k = \frac{y}{x}$$

constant of variation,  $k \neq 0$

Example:

$$y = 3x \text{ or } 3 = \frac{y}{x}$$



The graph of all points describing a direct variation is a line passing through the origin.

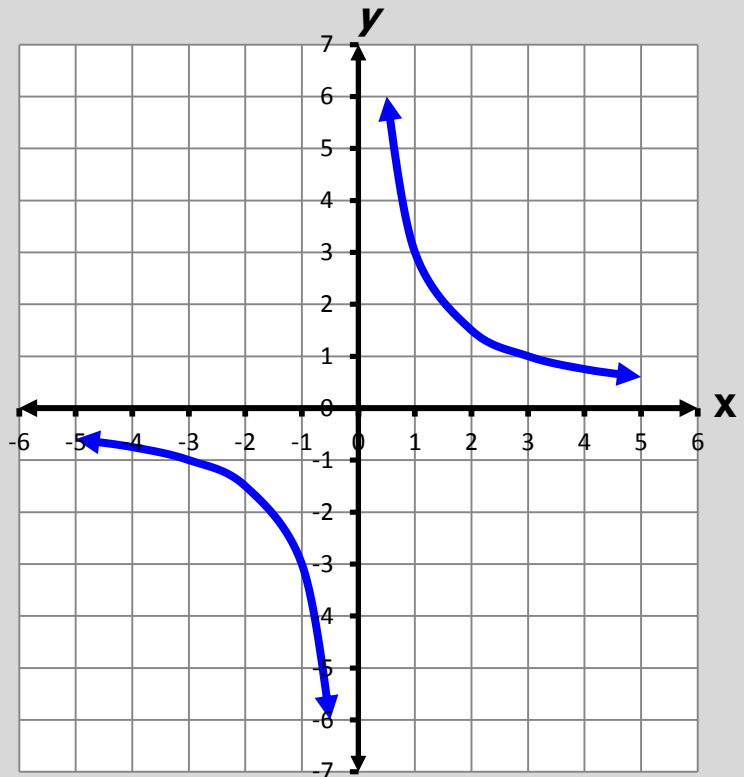
# Inverse Variation

$$y = \frac{k}{x} \quad \text{or} \quad k = xy$$

constant of variation,  $k \neq 0$

Example:

$$y = \frac{3}{x} \quad \text{or} \quad xy = 3$$



The graph of all points describing an inverse variation relationship are 2 curves that are reflections of each other.



# Statistics Notation

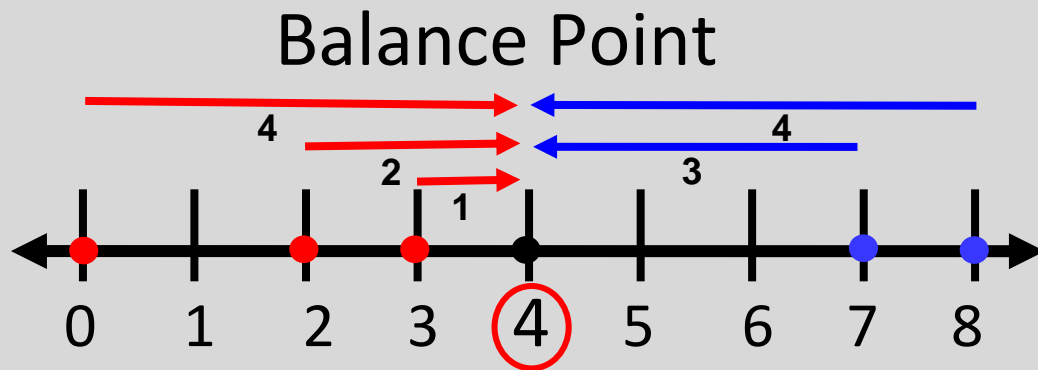
$x_i$	$i^{\text{th}}$ element in a data set
$\mu$	mean of the data set
$\sigma^2$	variance of the data set
$\sigma$	standard deviation of the data set
$n$	number of elements in the data set

# Mean

A measure of central tendency

Example: Find the mean of the given data set.

Data set: 0, 2, 3, 7, 8



Numerical Average

$$\mu = \frac{0 + 2 + 3 + 7 + 8}{5} = \frac{20}{5} = 4$$

# Median

A measure of central tendency

Examples:

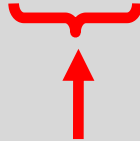
Find the median of the given data sets.

Data set: 6, 7, 8, 9, 9



The median is 8.

Data set: 5, 6, 8, 9, 11, 12



The median is 8.5.

# Mode

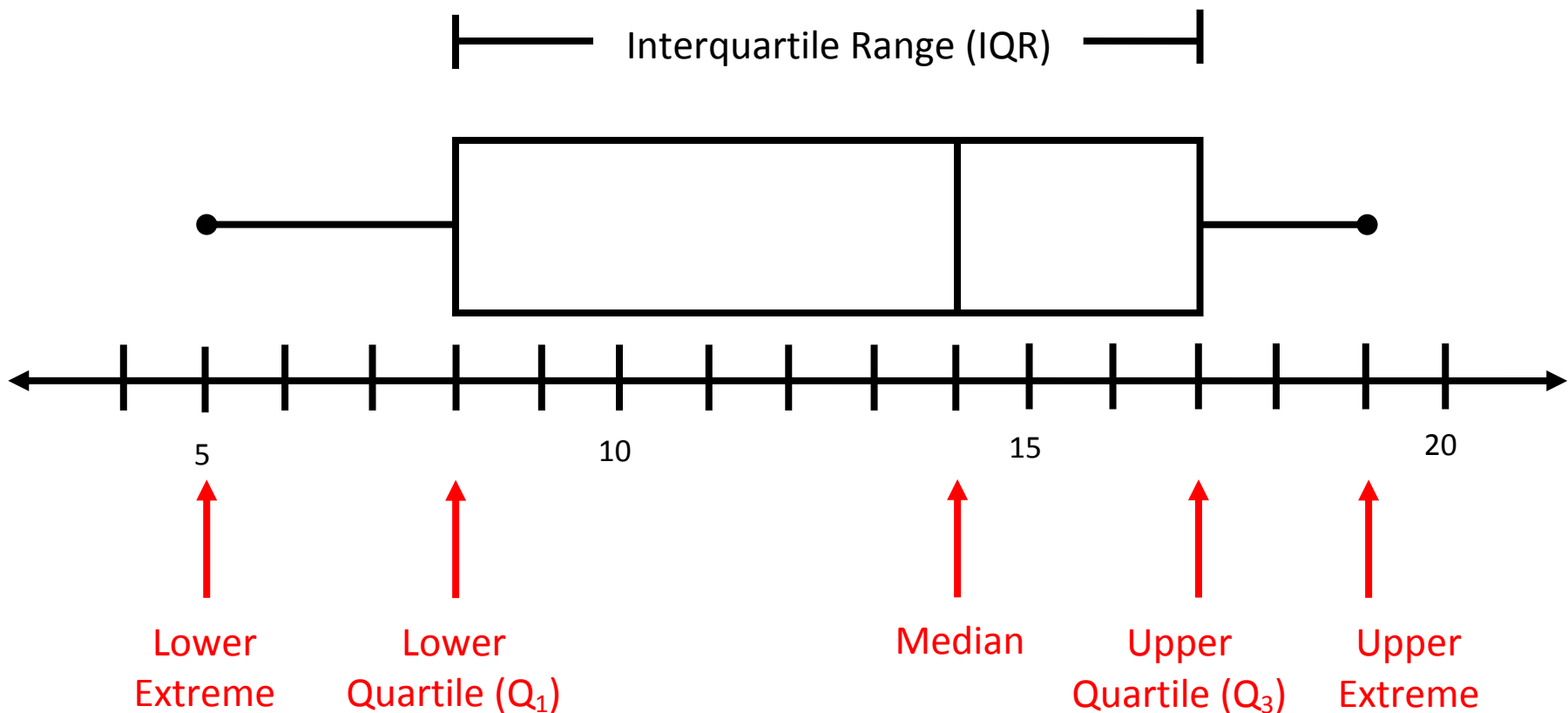
A measure of central tendency

Examples:

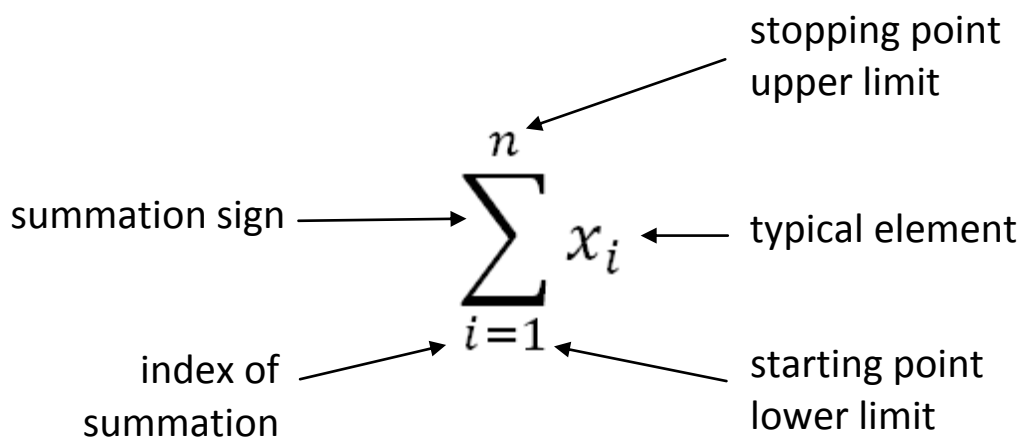
Data Sets	Mode
3, 4, 6, 6, 6, 6, 10, 11, 14	6
0, 3, 4, 5, 6, 7, 9, 10	none
5.2, 5.2, 5.2, 5.6, 5.8, 5.9, 6.0	5.2
1, 1, 2, 5, 6, 7, 7, 9, 11, 12	1, 7 bimodal

# Box-and-Whisker Plot

A graphical representation of the **five-number** summary



# Summation



This expression means sum the values of  $x$ , starting at  $x_1$  and ending at  $x_n$ .

$$\sum_{i=1}^n x_i = x_1 + x_2 + x_3 + \dots + x_n$$

Example: Given the data set  $\{3, 4, 5, 5, 10, 17\}$

$$\sum_{i=1}^6 x_i = 3 + 4 + 5 + 5 + 10 + 17 = 44$$

# Mean Absolute Deviation

A measure of the spread of a data set

$$\begin{array}{l} \text{Mean} \\ \text{Absolute} \\ \text{Deviation} \end{array} = \frac{\sum_{i=1}^n |x_i - \mu|}{n}$$

The mean of the sum of the absolute value of the differences between each element and the mean of the data set

# Variance

A measure of the spread of a data set

$$\text{variance}(\sigma^2) = \frac{\sum_{i=1}^n (x_i - \mu)^2}{n}$$

The mean of the squares of the differences between each element and the mean of the data set



# Standard Deviation

A measure of the spread of a data set

$$\text{standard deviation } (\sigma) = \sqrt{\frac{\sum_{i=1}^n (x_i - \mu)^2}{n}}$$

The square root of the mean of the squares of the differences between each element and the mean of the data set or the square root of the variance

# z-Score

The number of standard deviations an element is away from the mean

sw Snip Ctrl+N

$$\text{z-score } (z) = \frac{x - \mu}{\sigma}$$

where  $x$  is an element of the data set,  $\mu$  is the mean of the data set, and  $\sigma$  is the standard deviation of the data set.

**Example:** Data set A has a mean of 83 and a standard deviation of 9.74. What is the z-score for the element 91 in data set A?

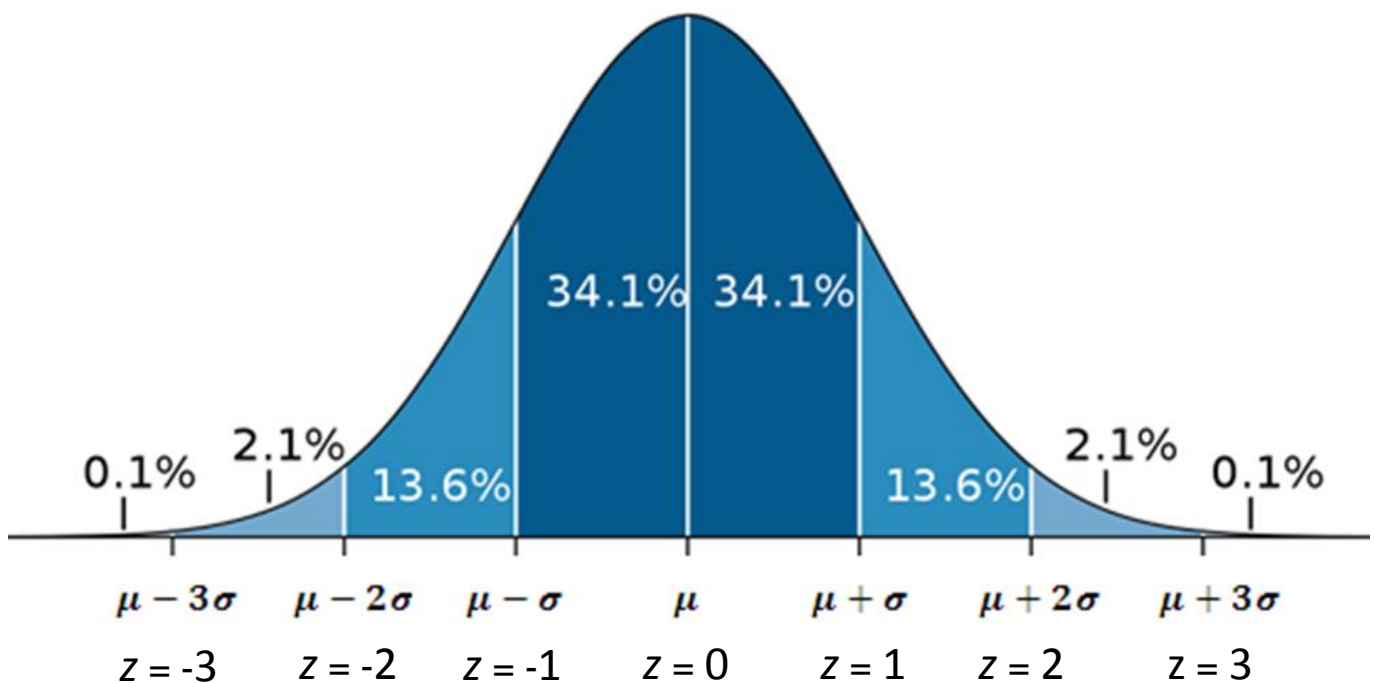
$$z = \frac{91-83}{9.74} = 0.821$$

# z-Score

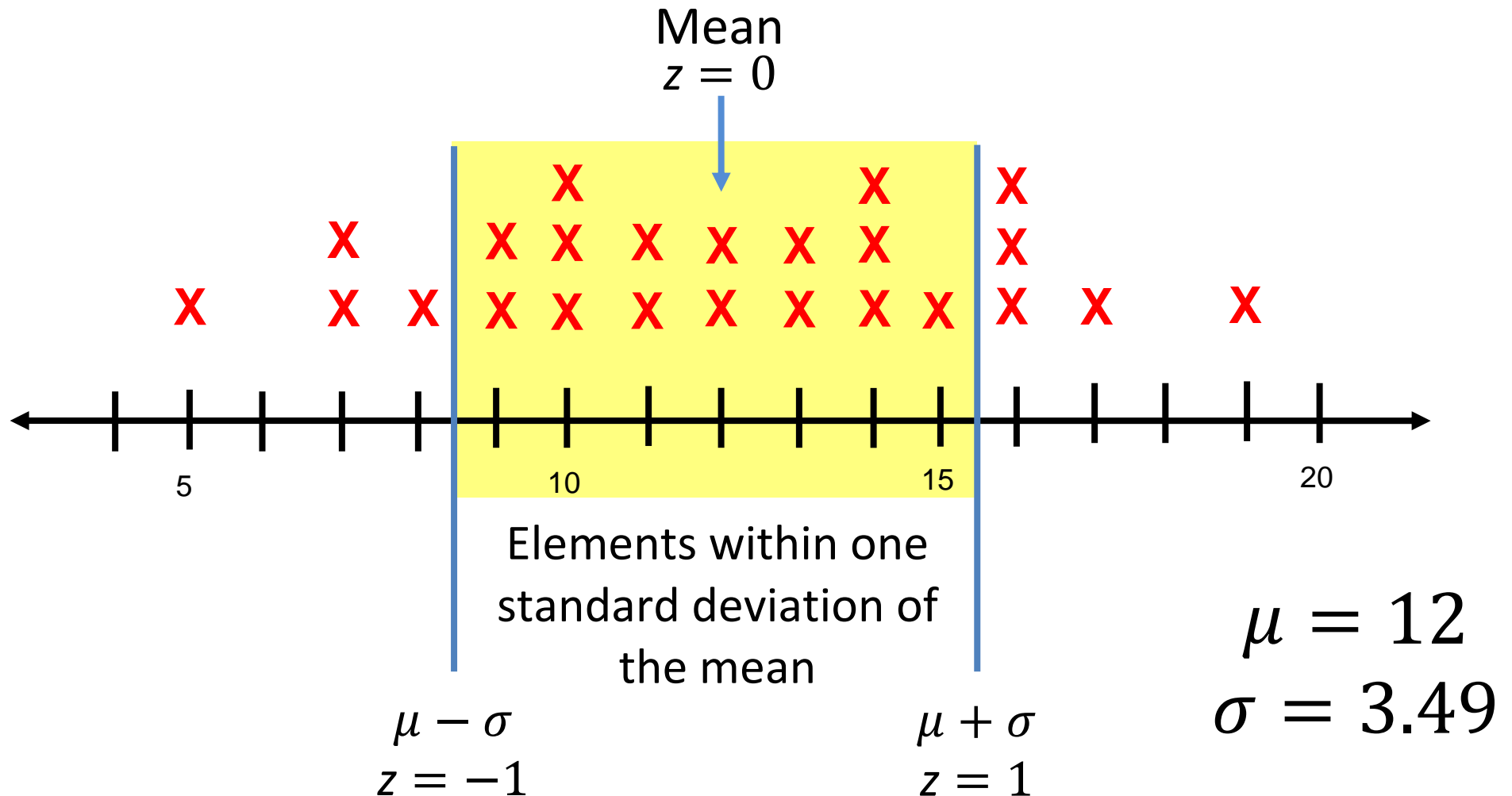
The number of standard deviations an element is from the mean

sw Snip Ctrl+N

$$\text{z-score } (z) = \frac{x - \mu}{\sigma}$$

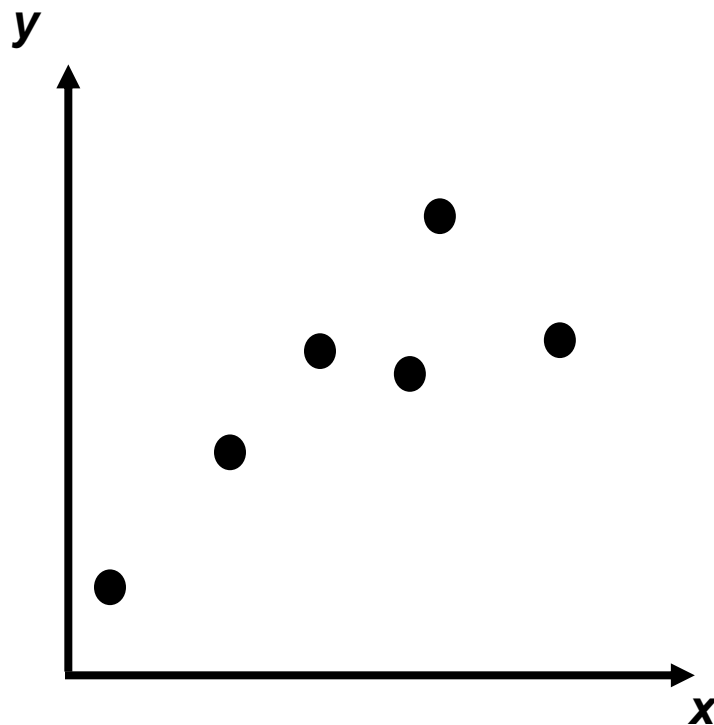


# Elements within One Standard Deviation ( $\sigma$ ) of the Mean ( $\mu$ )



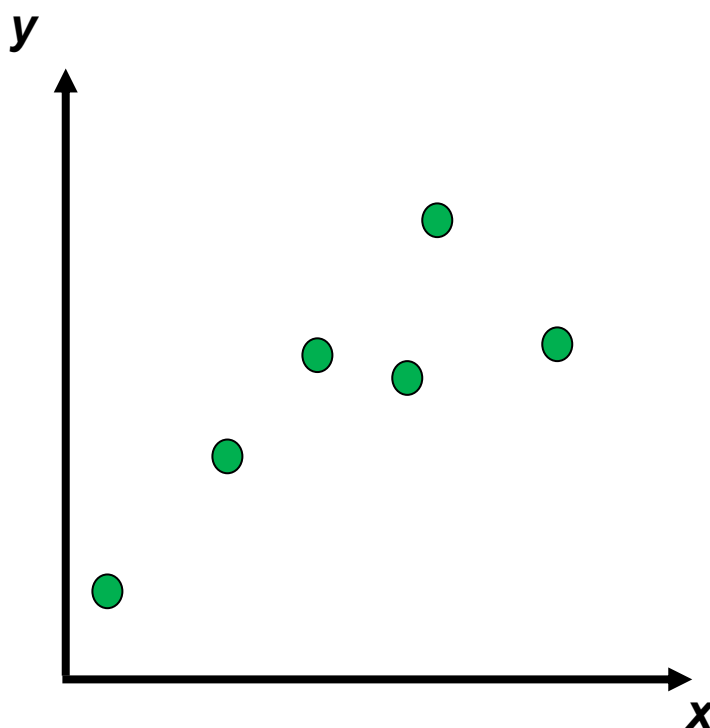
# Scatterplot

Graphical representation of the relationship between two numerical sets of data



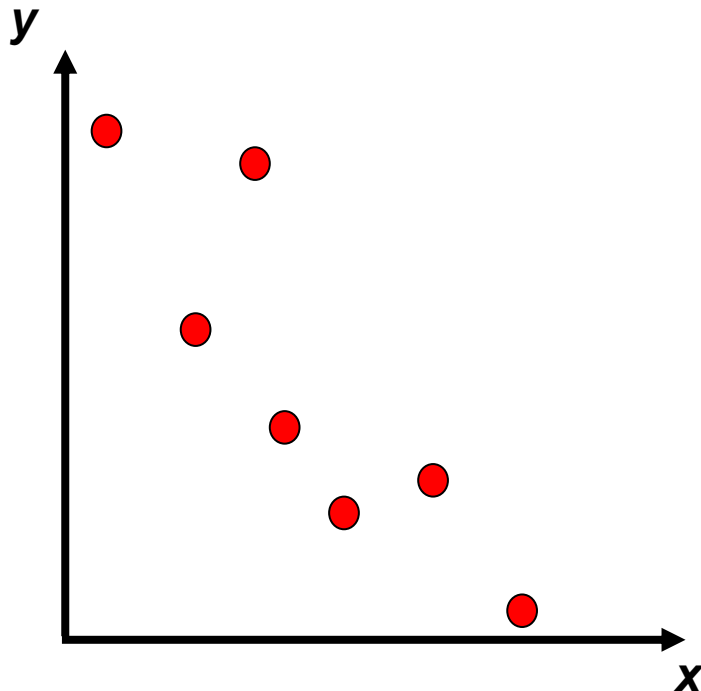
# Positive Correlation

In general, a relationship where the dependent ( $y$ ) values increase as independent values ( $x$ ) increase



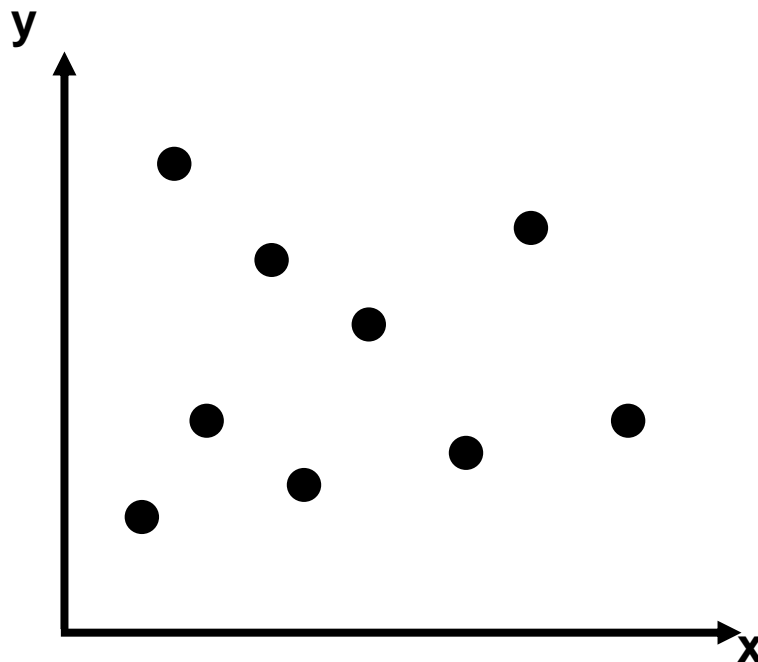
# Negative Correlation

In general, a relationship where the dependent ( $y$ ) values decrease as independent ( $x$ ) values increase.



# No Correlation

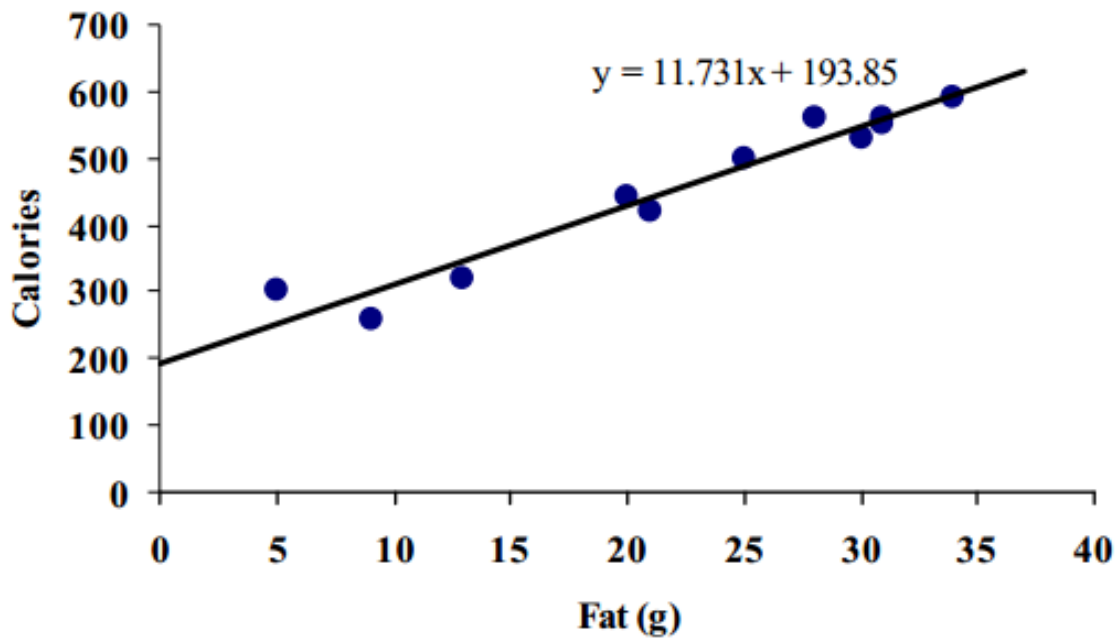
No relationship between the dependent ( $y$ ) values and independent ( $x$ ) values.



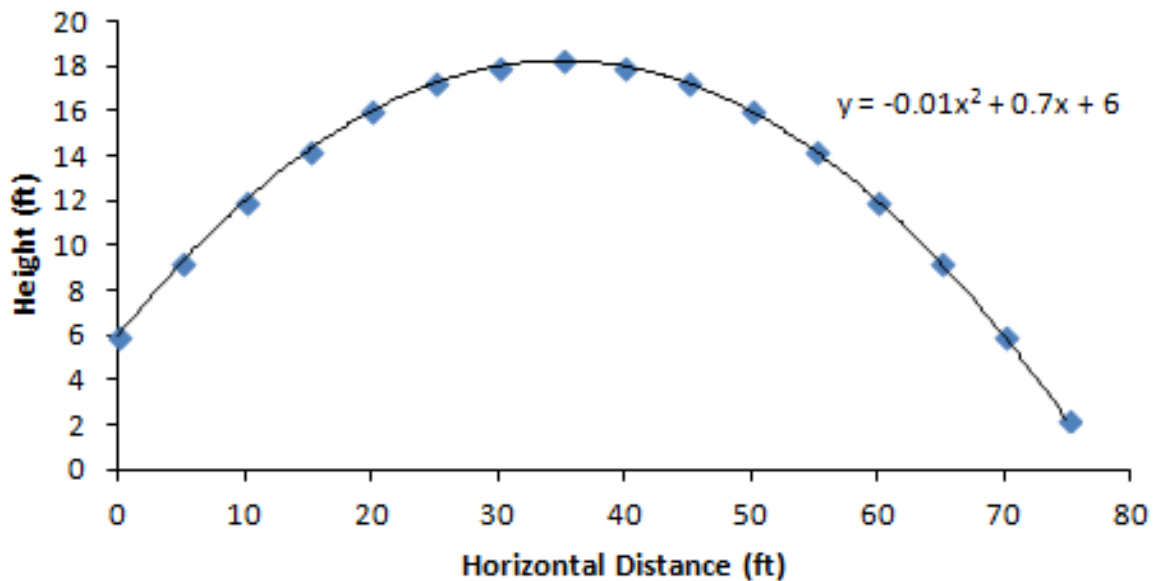


# Curve of Best Fit

## Calories and Fat Content



## Height of a Shot Put



# Outlier Data

